

中國科學院物理研究所  
Institute of Physics, Chinese Academy of Sciences



超导基础理论和实验技术讲座

National Lab for Superconductivity Lecture Series

【第100期】

# Anomalous Magnetic Moments as Evidence of Chiral Superconductivity in Bi/Ni Bilayer

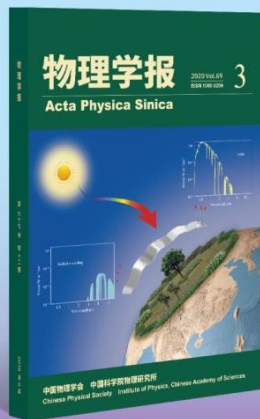
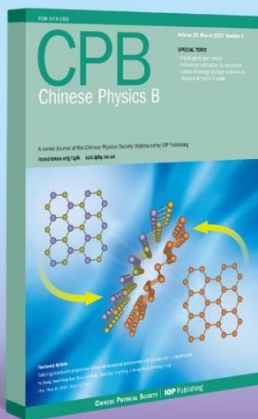
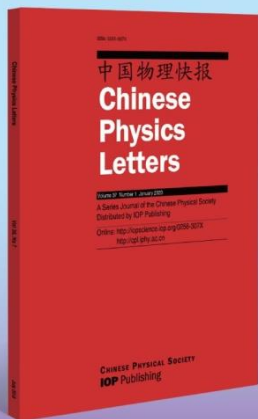
吕力

中国科学院物理研究所



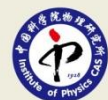
主办 中科院物理所超导国家重点实验室、学术服务部  
协办 《物理学报》 | CPL | CPB | 《物理》

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- ▶ CPL的 Express Letters 栏目对标 PRL, 质量高, 发表快, 国际推广。接收邮件投稿:  
[zhaiz@iphy.ac.cn](mailto:zhaiz@iphy.ac.cn)
- ▶ CPB和《物理学报》刊登中英文物理学优秀原创成果, 物理学前沿研究领域专题与综述。
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# 中船重工鹏力（南京）超低温技术有限公司

## CSIC PRIDE (NANJING) CRYOGENIC TECHNOLOGY CO.,LTD.

### 发展历程

- 2020年**

08 牵头承担国家重点研发计划重大仪器专项  
无液氦低温强磁场综合物性测量仪  
成功推出无液氦低温强磁场综合物性测量  
系统、低温真空泵
- 2018年**

07 成功研制1.5K无液氦低温系统  
开始研制稀释制冷机  
国家级博士后工作站申报获批
- 2016年**

06 GM低温制冷机实现MRI市场批量供货  
GM低温制冷机首次完成海外市场批量供货
- 2015年**

05 GM低温制冷机进军海外低温泵市场  
氦回收纯化液化设备实现产业化，应用于各大  
科研院所
- 2014年**

04 获批“高新技术企业”其中部分产品被  
认定为高新技术产品  
系列化低温设备在大科学工程领域得到  
良好应用
- 2013年**

03 加入中船重工，成立中船重工鹏力  
（南京）超低温技术有限公司
- 2011年**

02 首批氦回收纯化液化设备研制成功  
成功研制出4K/10K/77K系列低温设备，打  
破了国外垄断，保障了国内科研与军工领域的  
研究需求
- 2010年**

01 1月，成立，注册资金：3000万  
8月，成功研制出首套4.2K GM低温制冷机

### 公司定位

- 低温产品制造商
- 低温系统服务商



## 主要产品

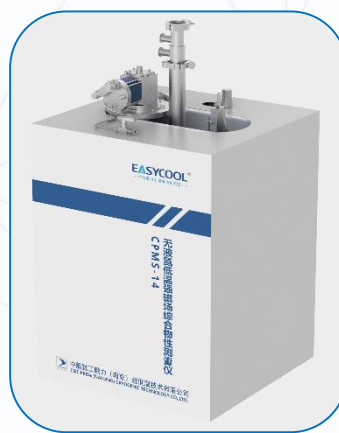
公司始终专注于GM低温制冷机、稀有气体提纯和液化装备、低温恒温器的研制和生产，同时也是一家提供全方位低温应用及解决方案的服务商。可为客户提供指标优异、性能稳定的低温产品。



GM低温制冷机



氮回收纯化液化装置



无液氮低温强磁场  
综合物性测量仪



稀释制冷机



(超) 低振动低温恒温器



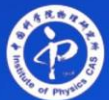
低温泵



1.5K低温系统



氮循环制冷装置



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# Anomalous Magnetic Moments as Evidence of Chiral Superconductivity in Bi/Ni Bilayer



吕力，中科院物理研究所研究员，主要从事低温凝聚态物理的实验研究，包括低维材料的电输运性质和热学性质研究、介观器件的制备和量子调控研究等。曾经担任物理所极端条件实验室、崔琦实验室、固态量子信息与计算实验室的主任，物理所副所长。目前是物理所怀柔研究部主任，同时也是中国物理学会出版工作委员会主任。2012年当选美国物理学会会士，2016年当选英国物理学会会士。

主办 中科院物理所超导国家重点实验室、学术服务部

协办 《物理学报》 | CPL | CPB | 《物理》

# Anomalous Magnetic Moments as Evidence of Chiral Superconductivity in Bi/Ni Epitaxial Bilayer

**Junhua Wang**, Guang Yang, Zhaozheng Lyu, Yuan Pang, Guangtong Liu,  
Zhongqing Ji, Jie Fan, Xiunian Jing, Changli Yang, Fanming Qu, Li Lu (吕力)  
*Institute of Physics, CAS, Beijing, China*

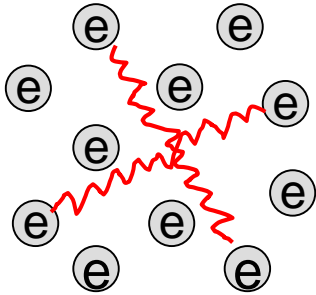
**Xinxin Gong** and **Xiaofeng Jin**  
*Fudan University, Shanghai, China*

# Conventional vs. Unconventional Superconductivity

## Conventional SC

**s-wave pairing**  
**zero angular momentum**

For extended electrons

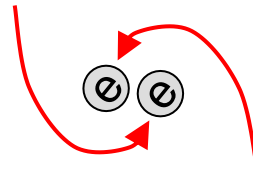


➤ Most known SCs

## Unconventional SC

**p-wave, d-wave, ...**  
**high angular momentum**

For electrons with  
more localized orbits  
compromise between  
attractive & repulsive  
interactions



- Strongly correlated electron systems
- Hard-core atoms:
  - superfluid  $^3\text{He-A}$
  - cold atoms

**Spinless, p-wave-like**  
... ..

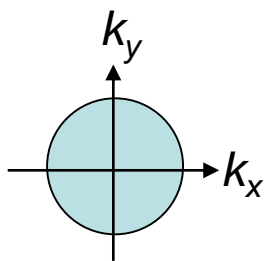
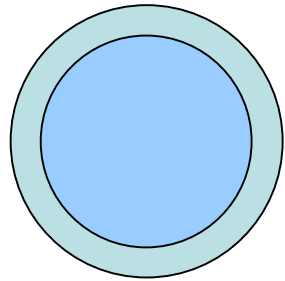
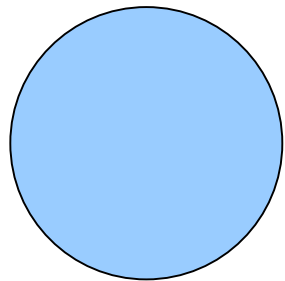
For electrons with  
strong SOC or spin-  
momentum locking

拓扑材料中的超导  
顾开元 罗天创 葛军 王健  
《物理学报》2020

Emerging topological  
superconductivity in  
new topological  
materials/hetrostruc.?

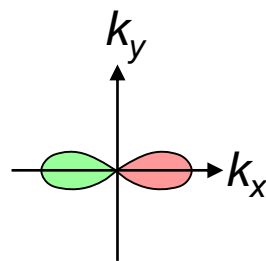
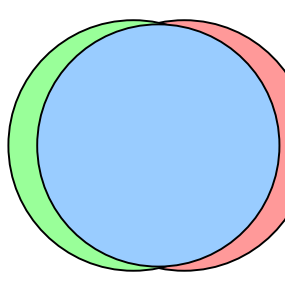
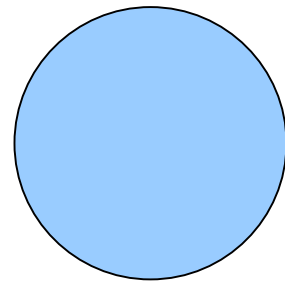
- Doped TIs, Weyl SM., Hybrid devices, ...
- TMDC
- ... ..

# Pairing Symmetry, Even/Odd Parity



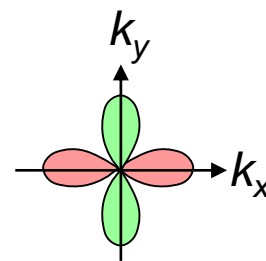
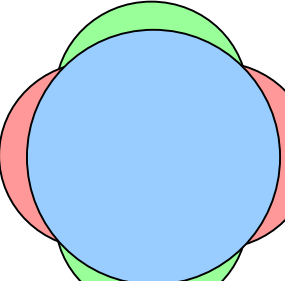
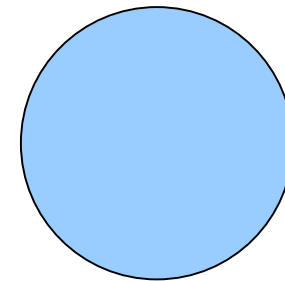
s-wave

$$|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



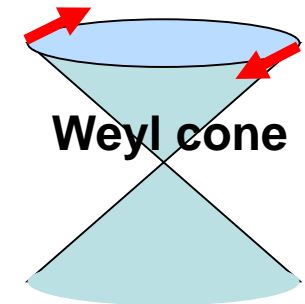
$p_x$ -wave

$$\begin{aligned} &|\uparrow\uparrow\rangle \\ &|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle \\ &|\downarrow\downarrow\rangle \end{aligned}$$

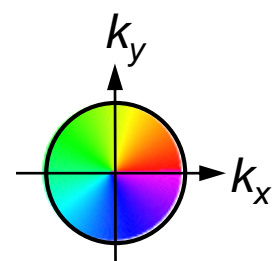
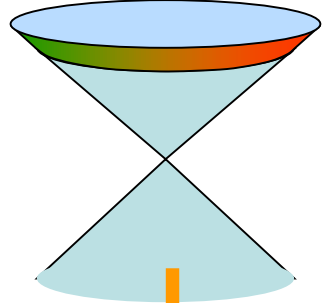


$d_{x^2-y^2}$

$$|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle$$



Weyl cone

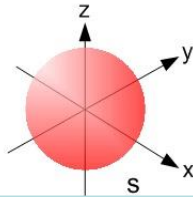
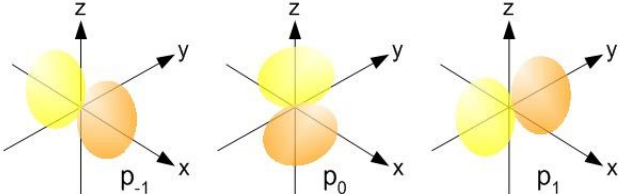
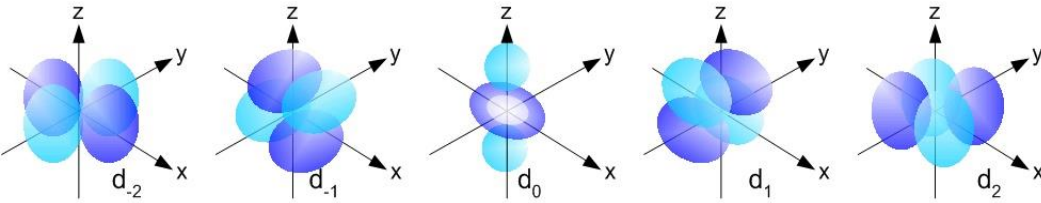
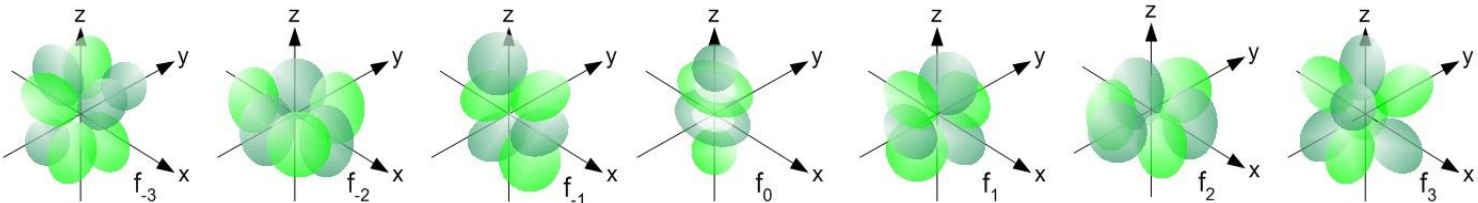


$p_x \pm ip_y$



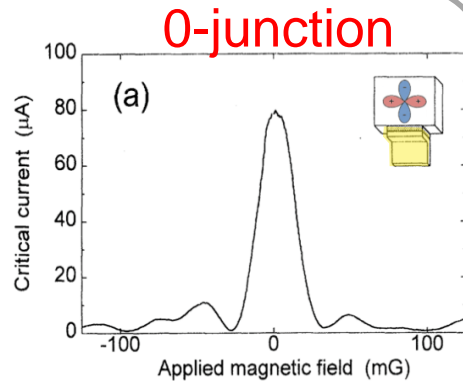
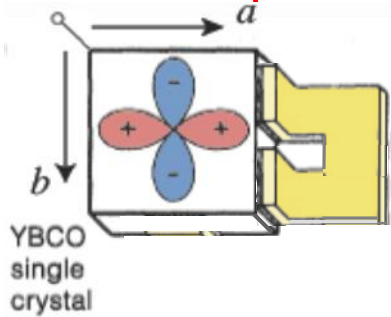
# Pairing Symmetry, Even/Odd Parity

库珀对波函数:  $\Psi = \Psi_{\text{质心}} \Psi_{\text{相对}} \Psi_{\text{自旋}}$

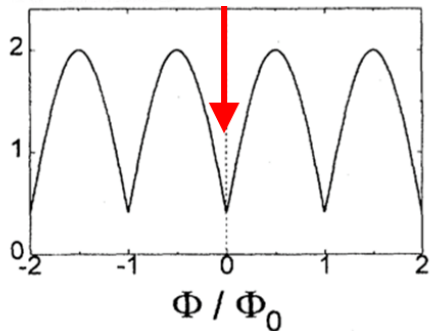
even		$s$	singlet: $ \uparrow\downarrow\rangle -  \downarrow\uparrow\rangle$
odd		$p_x, p_y, p_z$ $p_x + ip_x$	triplet: $ \uparrow\uparrow\rangle$ $ \uparrow\downarrow\rangle +  \downarrow\uparrow\rangle$ $ \downarrow\downarrow\rangle$
even		$d_{xy}$ $d_{x^2-y^2}$ $d_{xy} + id_{x^2-y^2}$	
odd			

# *d*-wave superconductivity in cuprates confirmed by phase-sensitive experiments

0-loop

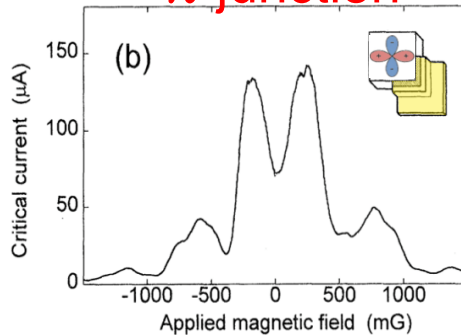


*d*-wave

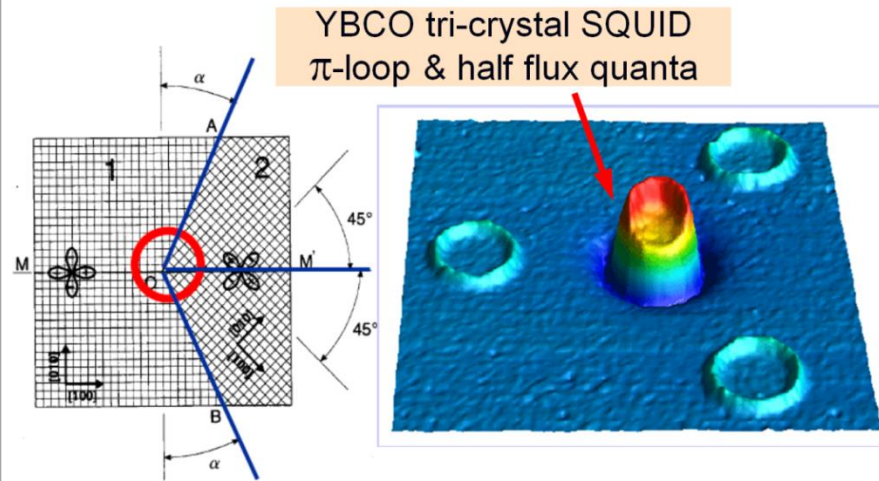


van Harlingen group

$\pi$ -junction



$\pi$ -loop in a tri-crystal ring



C. C. Tsuei group

Oliver E. Buckley Condensed Matter Physics Prize (1998)

# *p*-wave Superconductivity (Theory)

- Coexist. of SC and FM V. Ginzburg, 1956

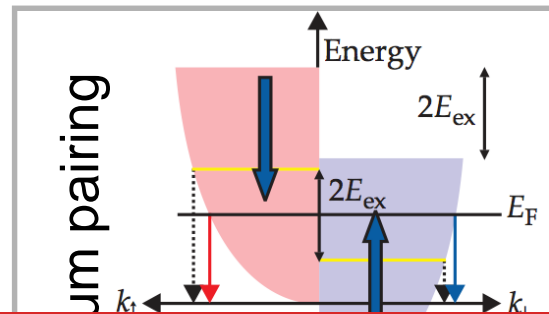
- Triplet pairing near SC-FM interface

FFLO mechanism

Fulde, Ferrell, PR' 1964,

Larkin, Ovchinnikov,

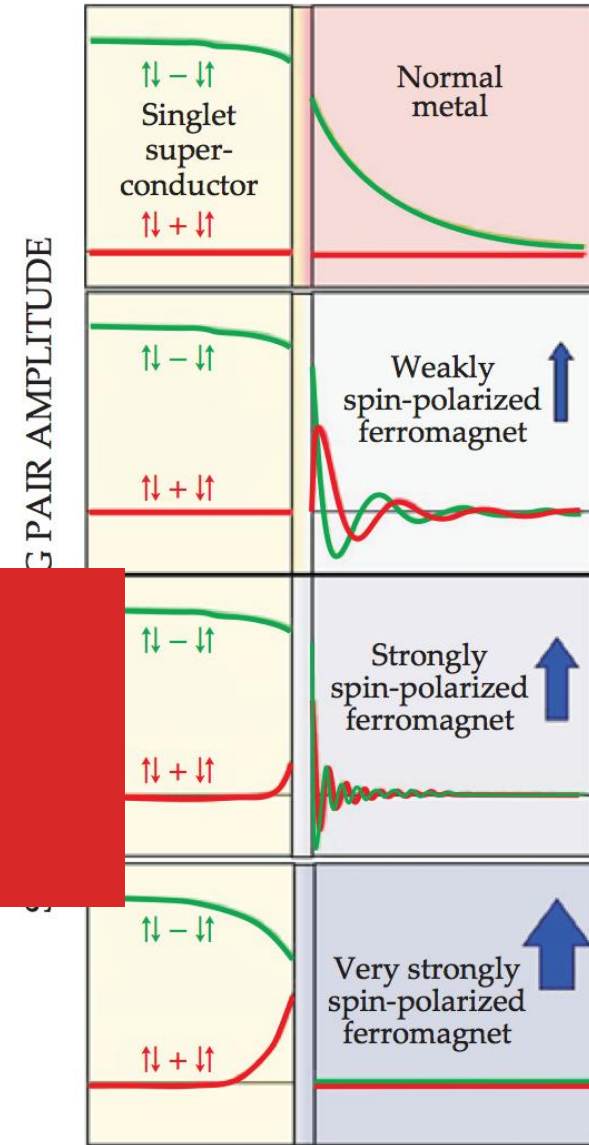
Sov. Phys. JETP' 1965



*p*-wave SC may coexist with magnetic ordering or magnetic fluctuations

- Magnetic fluctuation-mediated triplet pairing

Fay, Appel, PRB'1980



# $p$ -wave Superconductivity (Experimental)

- $^3\text{He-A}$  D. M. Lee, D. D. Osheroff and R. C. Richardson, 1971 + A. J. Leggett
- Heavy fermion superconductors:  
CeCu<sub>2</sub>Si<sub>2</sub>, UGe<sub>2</sub>, UPt<sub>3</sub>, URhGe, UCoGe, ... 30+
- ....

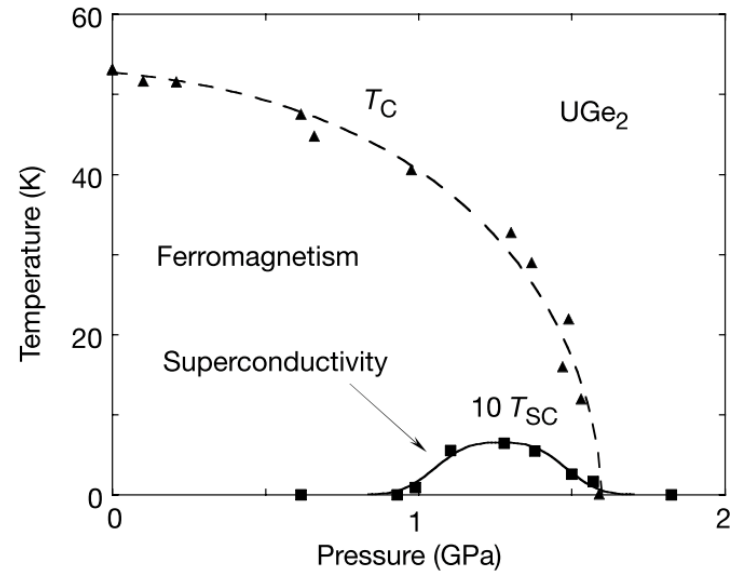
**Table I.** Selection of candidates of spin-triplet superconductors. HF: heavy fermion superconductors, NCS: Noncentrosymmetric superconductors, FM: ferromagnetic superconductors, \*: superconductivity under pressure.

Materials	Classification	Spin evidence of triplet pairing	Properties
$^3\text{He}$	Superfluid	magnetization, NMR etc. <sup>7)</sup>	$p$ -wave, A phase is chiral
Sr <sub>2</sub> RuO <sub>4</sub>	Oxide	NMR, polarized neutron	2D analogue of $^3\text{He-A}$ Chiral $p$ -wave
UPt <sub>3</sub>	HF	NMR <sup>18)</sup>	$f$ -wave
UBe <sub>13</sub> , URu <sub>2</sub> Si <sub>2</sub> , UNi <sub>2</sub> Al <sub>3</sub>	HF	NMR <sup>13)</sup>	
UGe <sub>2</sub> *, URhGe, UCoGe	FM, HF	Indirect	Anomalous $H_{c2}$ <sup>19-22)</sup>
UIr*	NCS, FM, HF	Indirect	
CeIrSi <sub>3</sub> *	NCS, HF	NMR <sup>23)</sup>	
Li <sub>2</sub> Pt <sub>3</sub> B	NCS	NMR <sup>24)</sup>	
CePt <sub>3</sub> Si	NCS, HF	Indirect	
CeRhSi <sub>3</sub> *	NCS, HF	Indirect	Anomalous $H_{c2}$ <sup>25)</sup>
S/FM/S	Junctions	Indirect ( $I_c$ ) <sup>26-29)</sup>	Odd-freq., even-parity, $s$ -wave

# $p$ -wave Superconductivity (Experimental)

Anomalous properties in:

- ✓ heat capacity
- ✓ magnetic susceptibility
- ✓ penetration depth
- ✓ NMR
- ✓ . . . . .

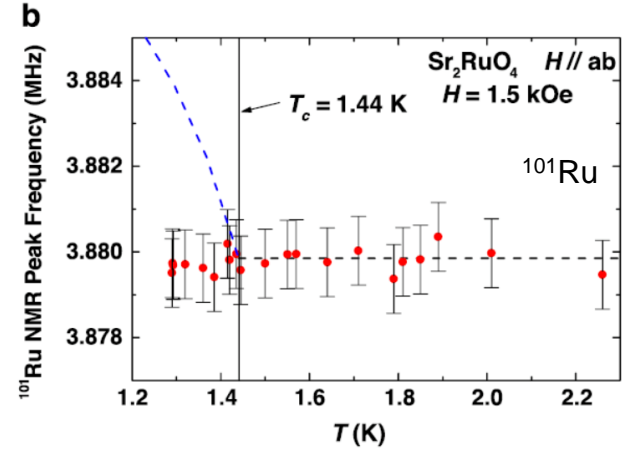
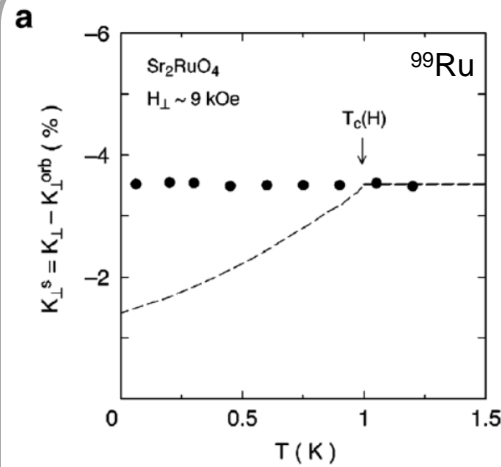
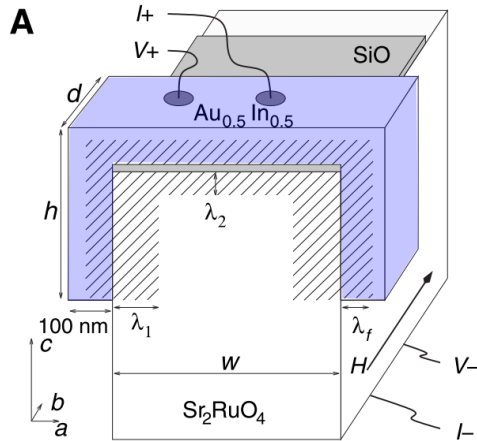


S. Saxena, et al., Nature' 2000.

**Needs to rule out:**

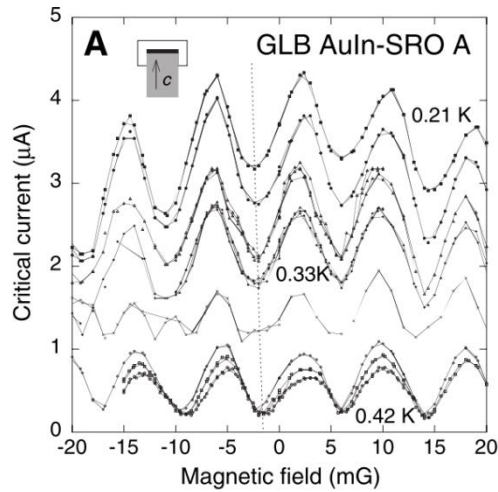
- local phase separation,
- inhomogeneity
- . . . . .

# Sr<sub>2</sub>RuO<sub>4</sub>: $p_x+ip_y$ -wave SC candidate?

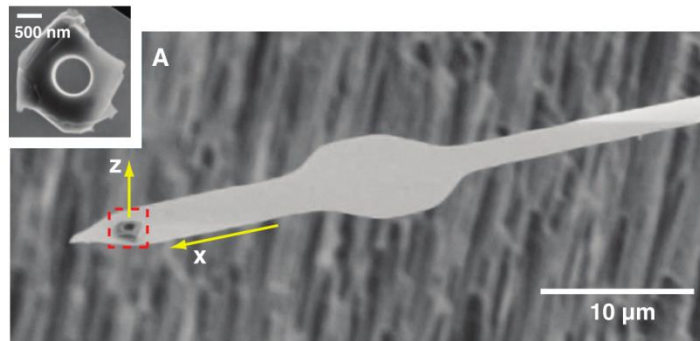


K. Ishida et al. PRB' 01

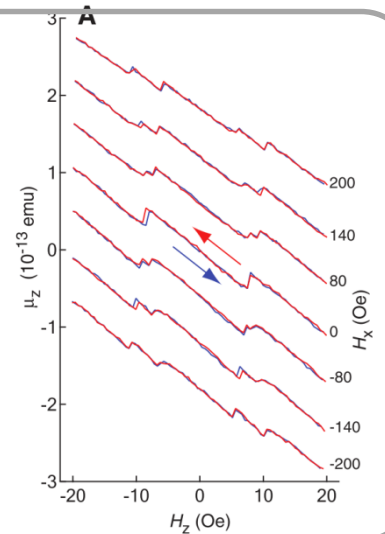
H. Murakawa et al. JPSJ' 07



Y. Liu, Maeno, Science 2004

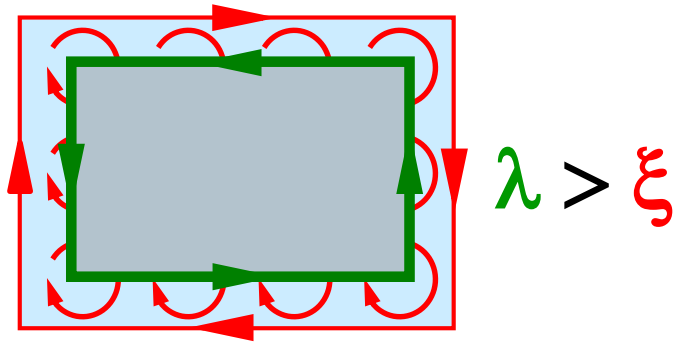


Budakian, Maeno, Science 2011



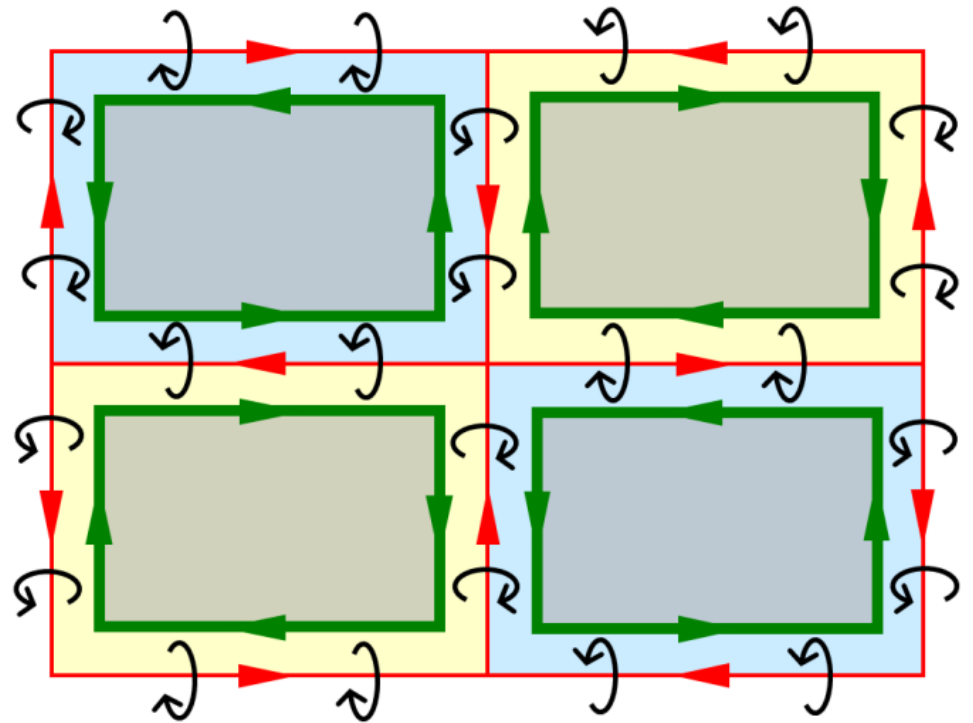
# Chiral $p_x+ip_y$ pairing, more features to expect

- Edge currents & Edge magnetization

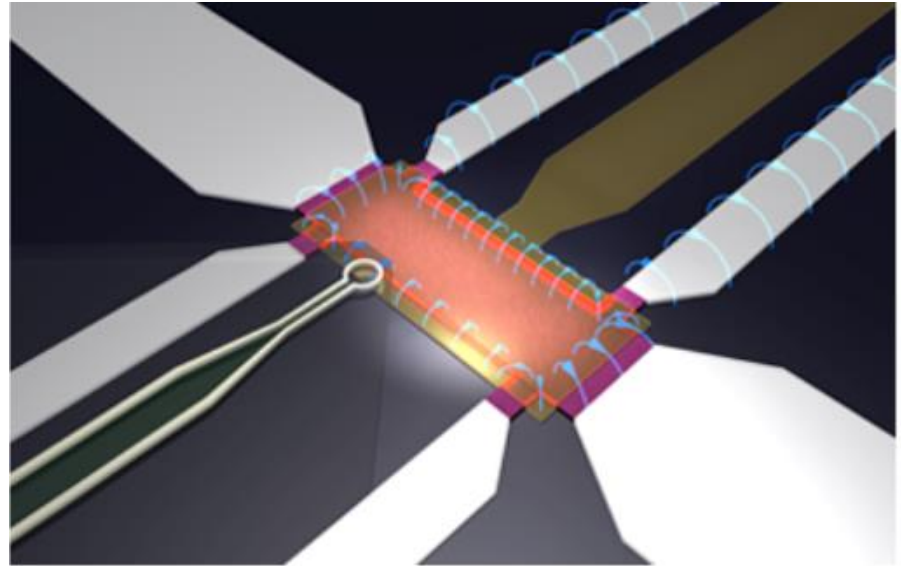
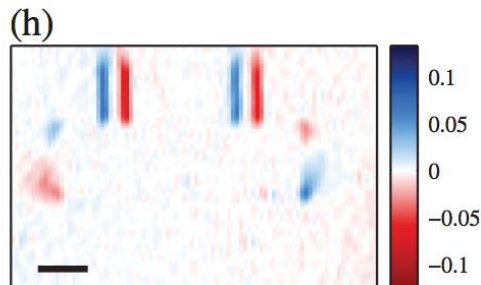
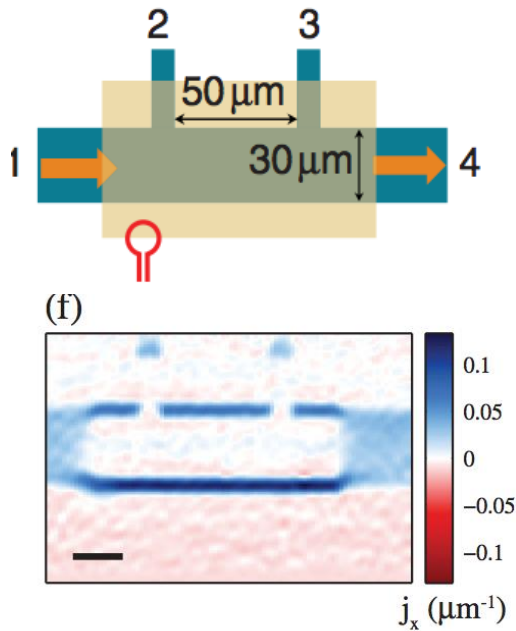


M. Sigrist, T. M. Rice, K. Ueda,  
PRL 63, 1727 (1989)

- Superconducting domains



# Search for edge magnetization in $\text{Sr}_2\text{RuO}_4$



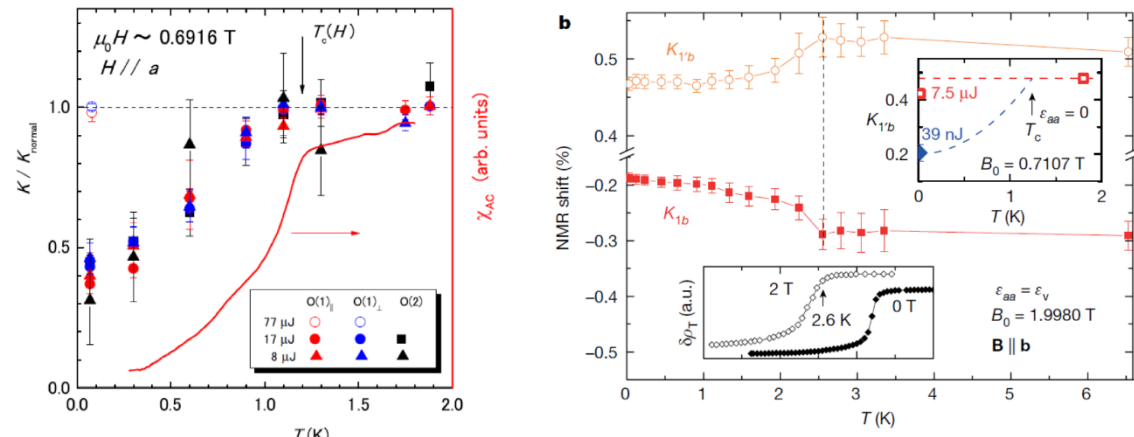
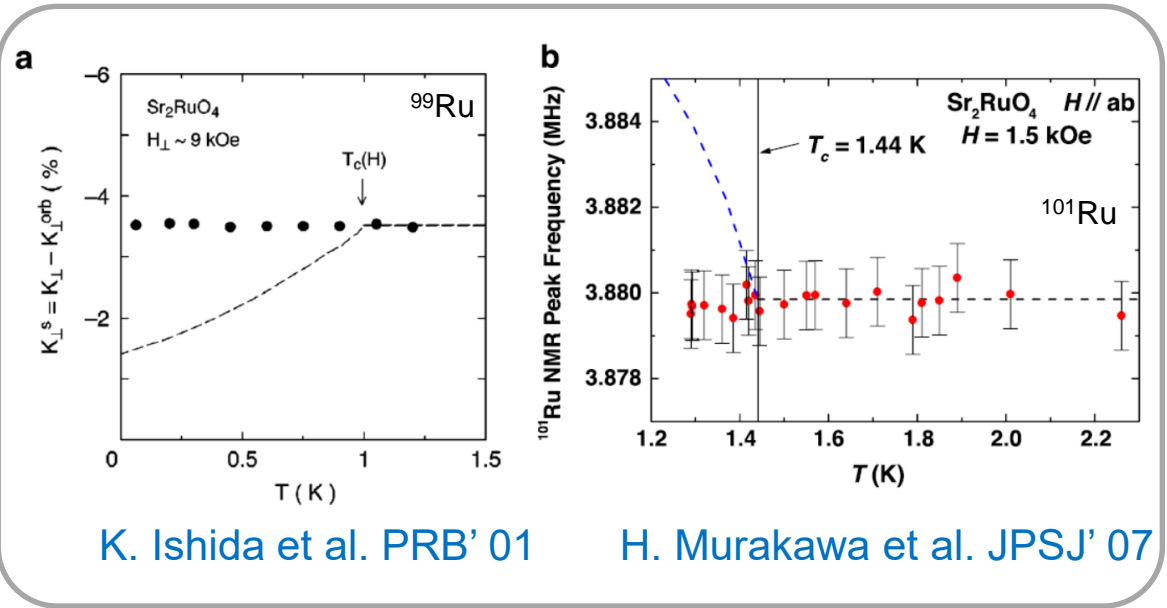
The Moler Group at Stanford University is a mesoscopic magnetic imaging lab in the departments of Physics and Applied Physics at Stanford University.

Fail to observe edge current and/or edge magnetization

Phys. Rev. B 72, 012504 (2005)  
Phys. Rev. B 76, 014526 (2007)  
Phys. Rev. B 81, 214501 (2010)



# Sr<sub>2</sub>RuO<sub>4</sub>: $p_x+ip_y$ -wave SC candidate?



K. Ishida et al., JPSJ' 2020

A. Pustogow et al., Nature' 2019

# $\text{Sr}_2\text{RuO}_4$ : $p_x+ip_y$ -wave SC candidate?

REVIEW ARTICLE      OPEN

## Even odder after twenty-three years: the superconducting order parameter puzzle of $\text{Sr}_2\text{RuO}_4$

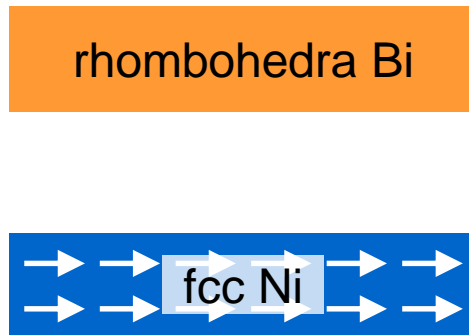
Andrew P. Mackenzie<sup>1,2</sup>, Thomas Scaffidi<sup>3</sup>, Clifford W. Hicks<sup>1</sup> and Yoshiteru Maeno<sup>4</sup>

In this short review, we aim to provide a topical update on the status of efforts to understand the superconductivity of  $\text{Sr}_2\text{RuO}_4$ . We concentrate on efforts to identify a superconducting order parameter symmetry that is compatible with all the major pieces of experimental knowledge of the material, and highlight some major discrepancies that have become even clearer in recent years. As the pun in the title suggests, we have tried to start the discussion from scratch, making no assumptions even about fundamental issues such as the parity of the superconducting state. We conclude that no consensus is currently achievable in  $\text{Sr}_2\text{RuO}_4$ , and that the reasons for this go to the heart of how well some of the key probes of unconventional superconductivity are really understood. This is, therefore, a puzzle that merits continued in-depth study.

*npj Quantum Materials* (2017)2:40; doi:10.1038/s41535-017-0045-4

# Bi/Ni bilayer

- J. S. Moodera et al, PRB 42, 179 (1990).
- P. LeClair, J. S. Moodera, J. Philip, and D. Heiman, PRL 94 037006 (2005).

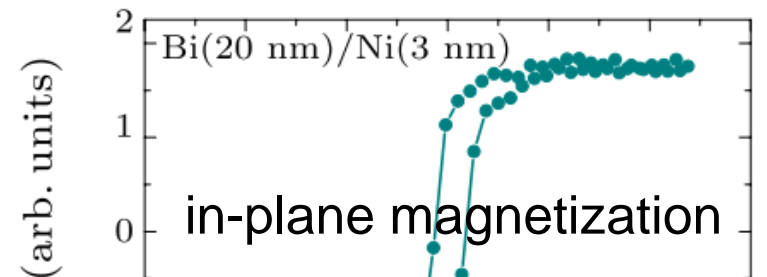
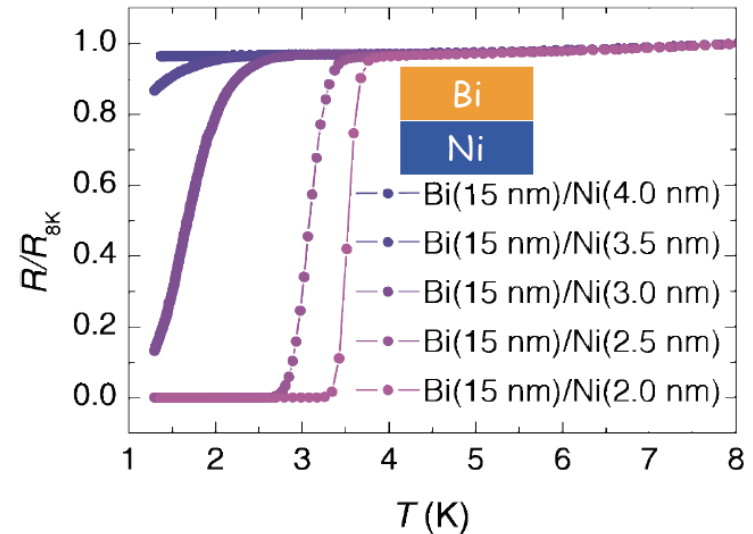
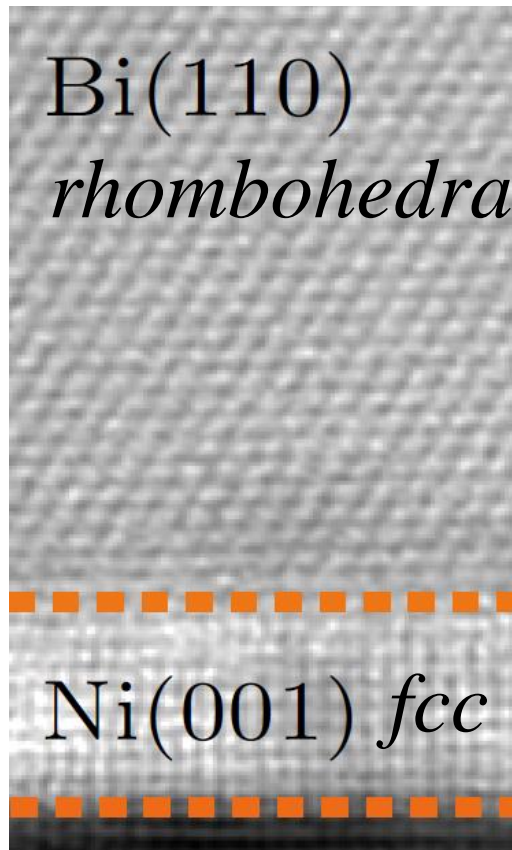


- Superconducting,  $T_c \approx 4.2$  K
- Coexistence of SC and FM

The SC was believed to arise from ~~fcc-phase Bi~~ induced by Ni.

# Bi/Ni epitaxial bilayer from Fudan U

X.F. Jin group  
at Fudan U

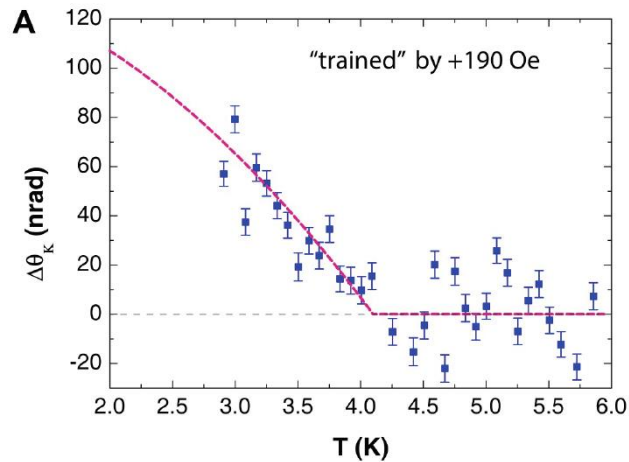


The superconductivity is likely unconventional, because it coexists with FM.

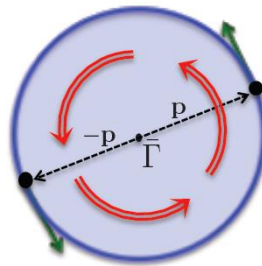
# Kerr Measurement based on Sagnac Interferometer

## Time-Reversal-Symmetry-Breaking Superconductivity in Epitaxial Bismuth/Nickel Bilayers

X.X. Gong et al., Sci. Adv. 3, e1602579 (2017)

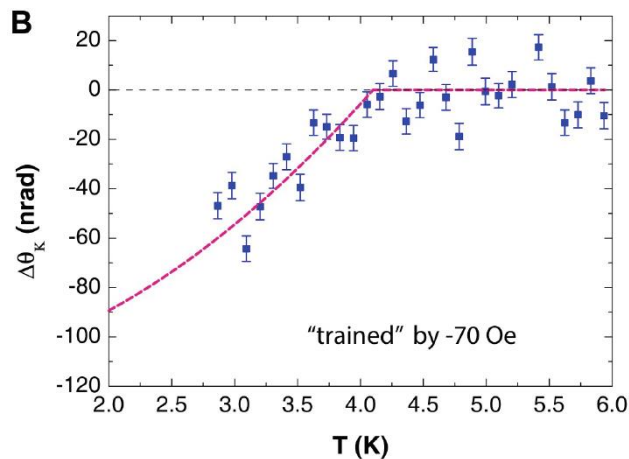


$H_{\text{training}} \odot$

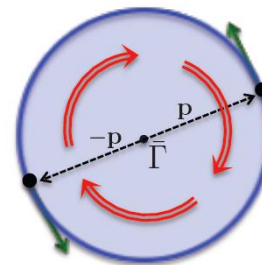


$$J_z = 2$$

$$d_{xy} + id_{x^2-y^2}$$

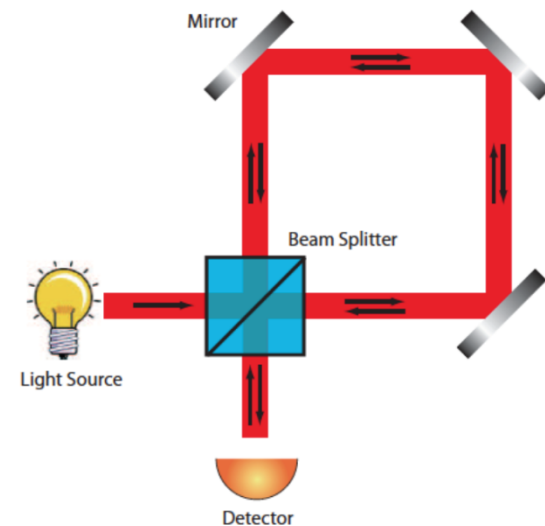


$H_{\text{training}} \otimes$

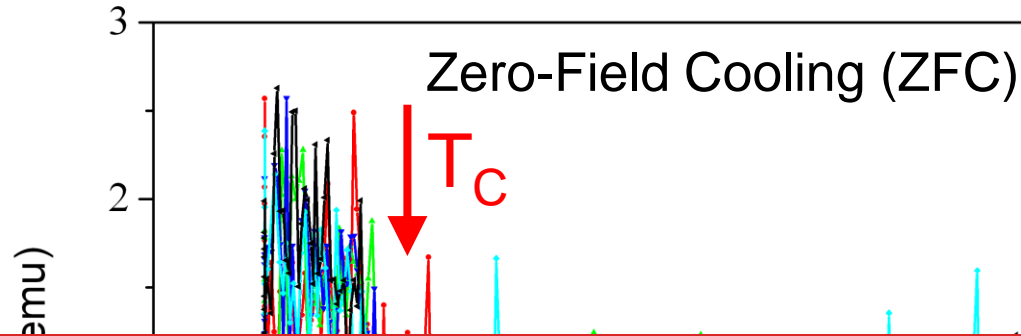


$$J_z = -2$$

$$d_{xy} - id_{x^2-y^2}$$



# SQUID VSM measurement: Anomalous out-of-plane magnetic moment arises below $T_c$



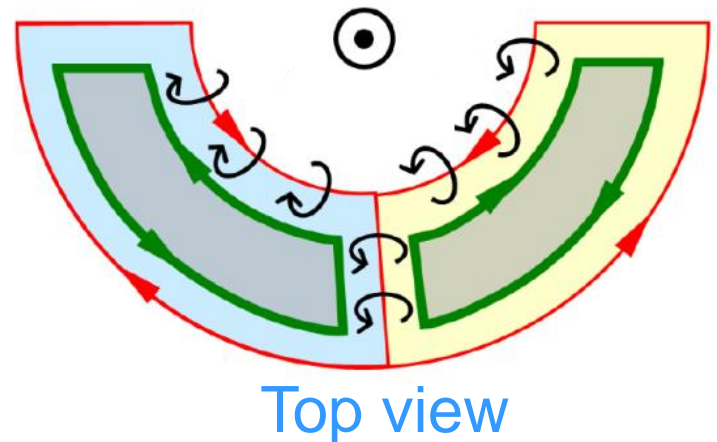
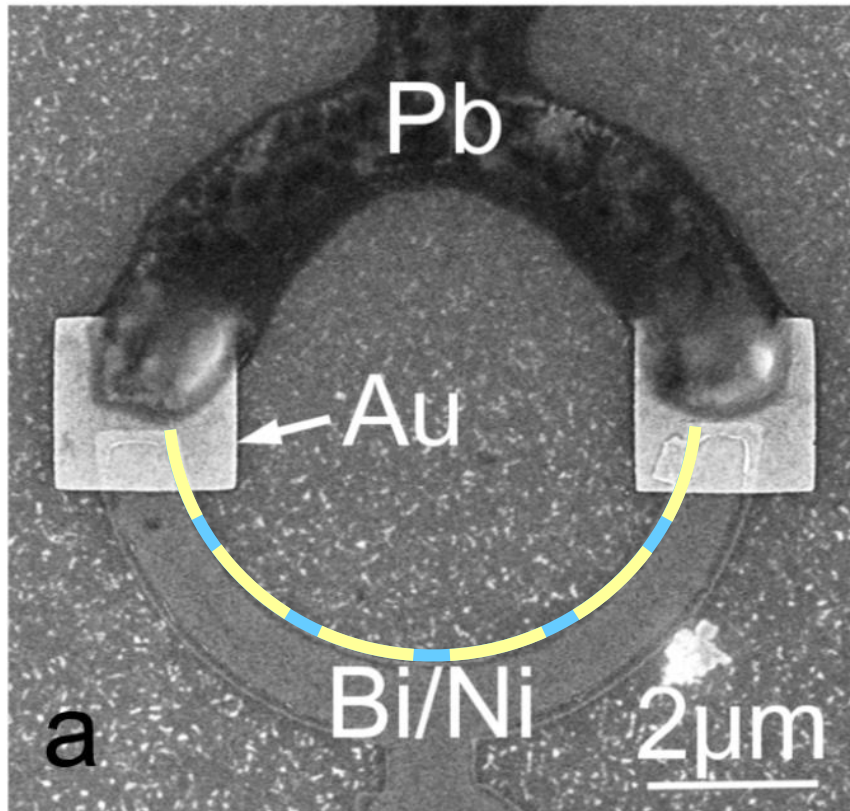
## The motivation of this work:

- What is the origin of this anomalous moment?
- Given the fact of SC and FM coexistence, could the moment arise from the orbital moments of Cooper pairs in a chiral superconductor?

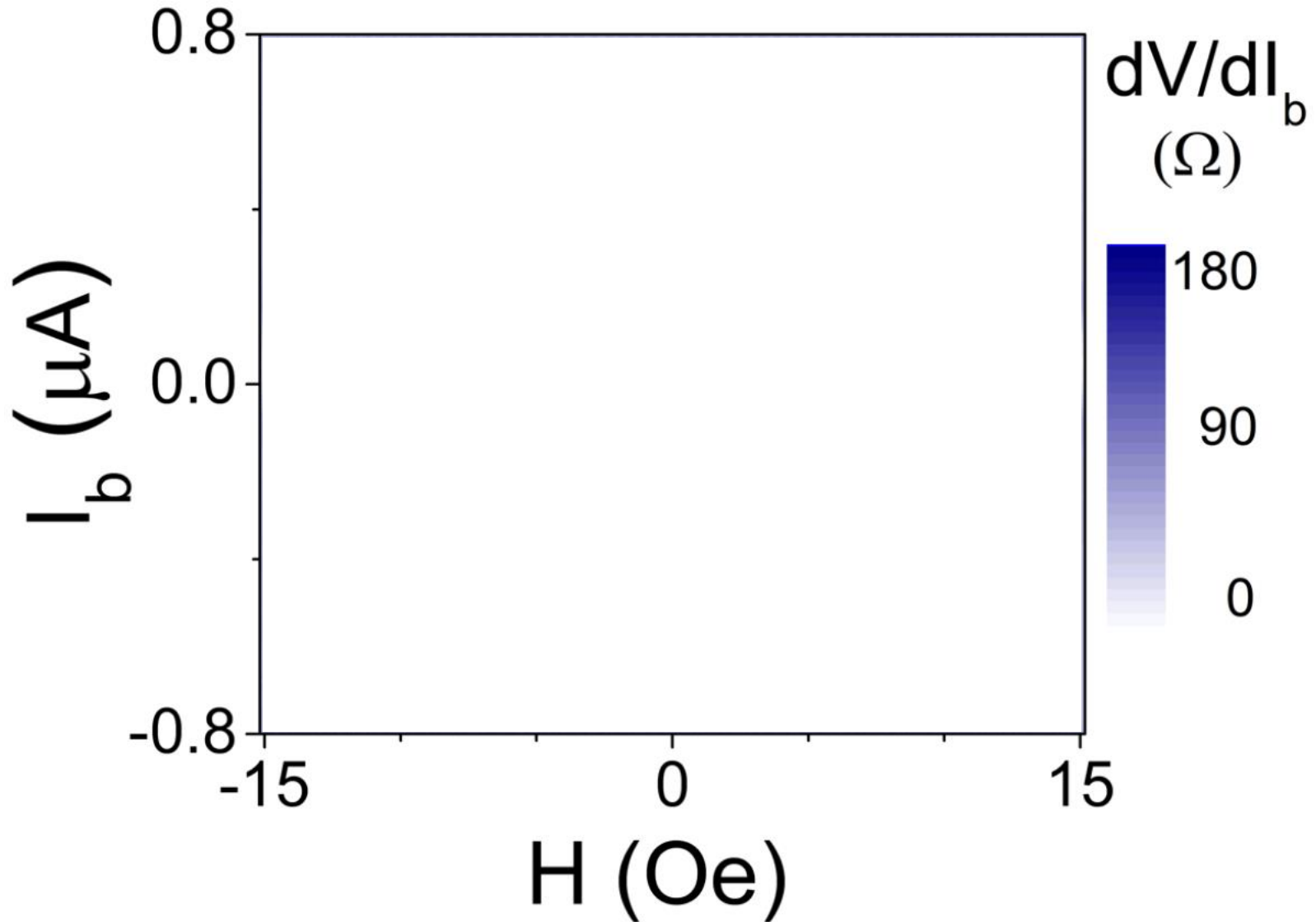
# Design of the experiment

Using Bi/Ni bilayer itself to form SQUIDs, to search for out-of-plane magnetic moments at the edges

dc SQUID

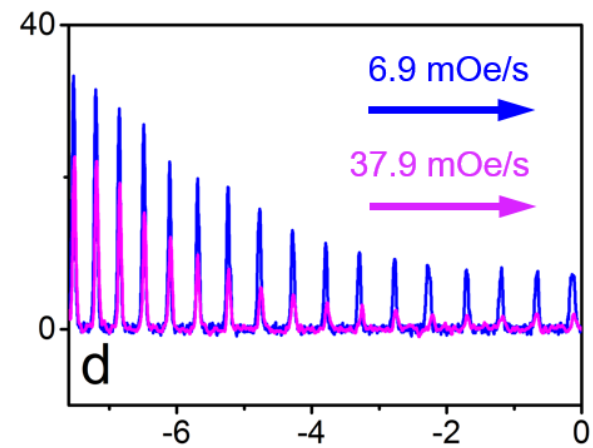
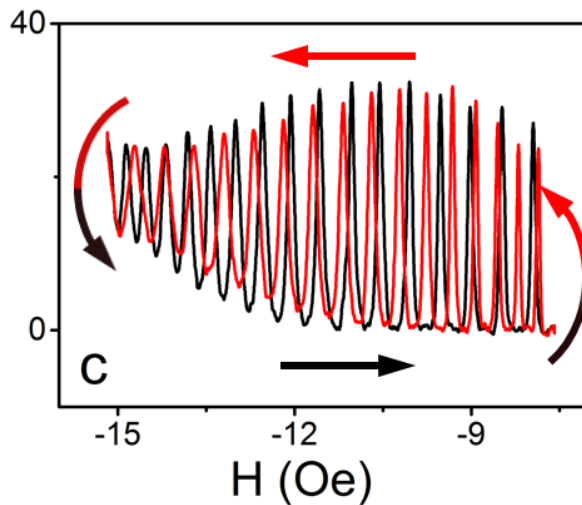
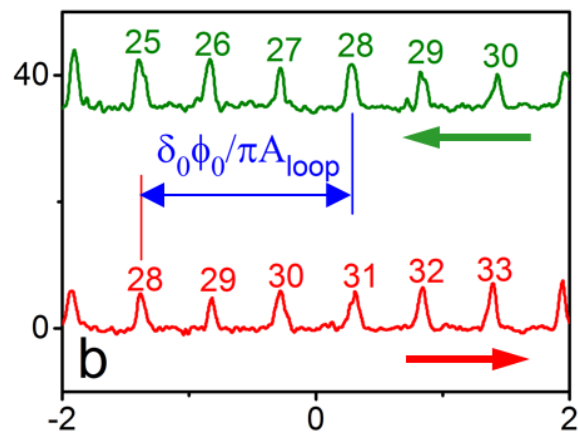
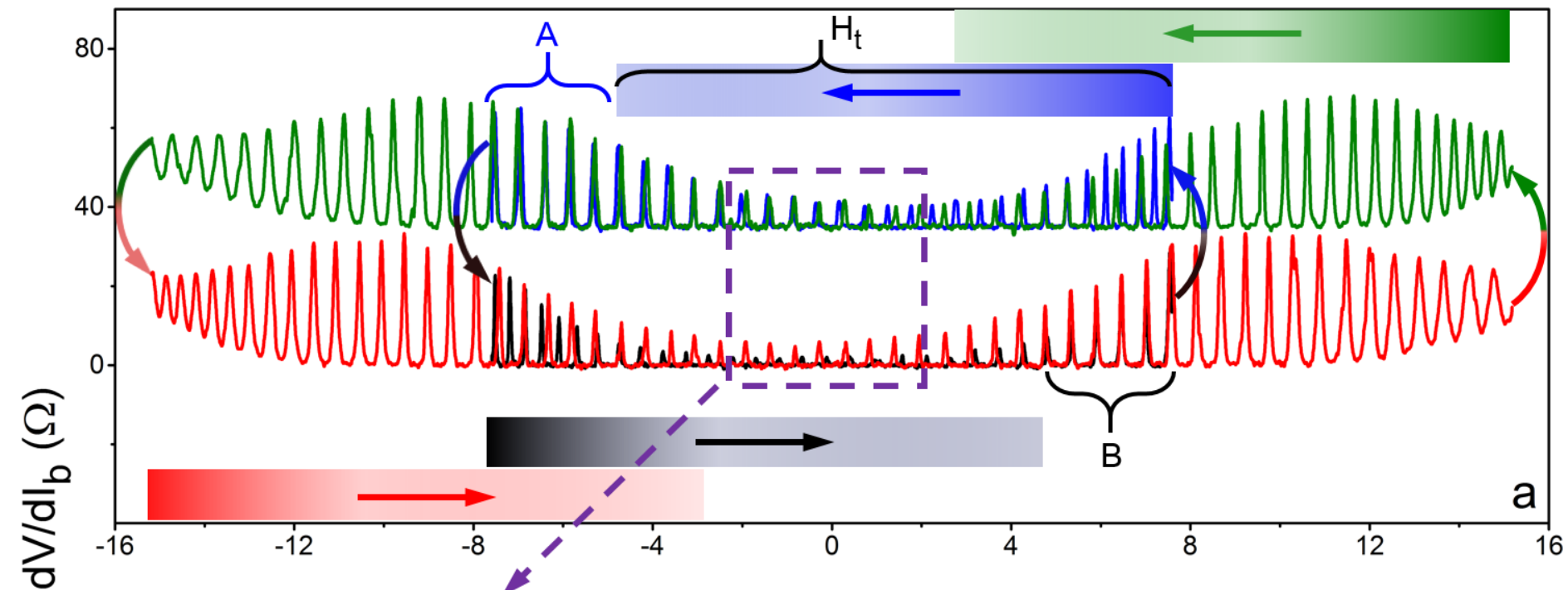


# Superconducting quantum interference

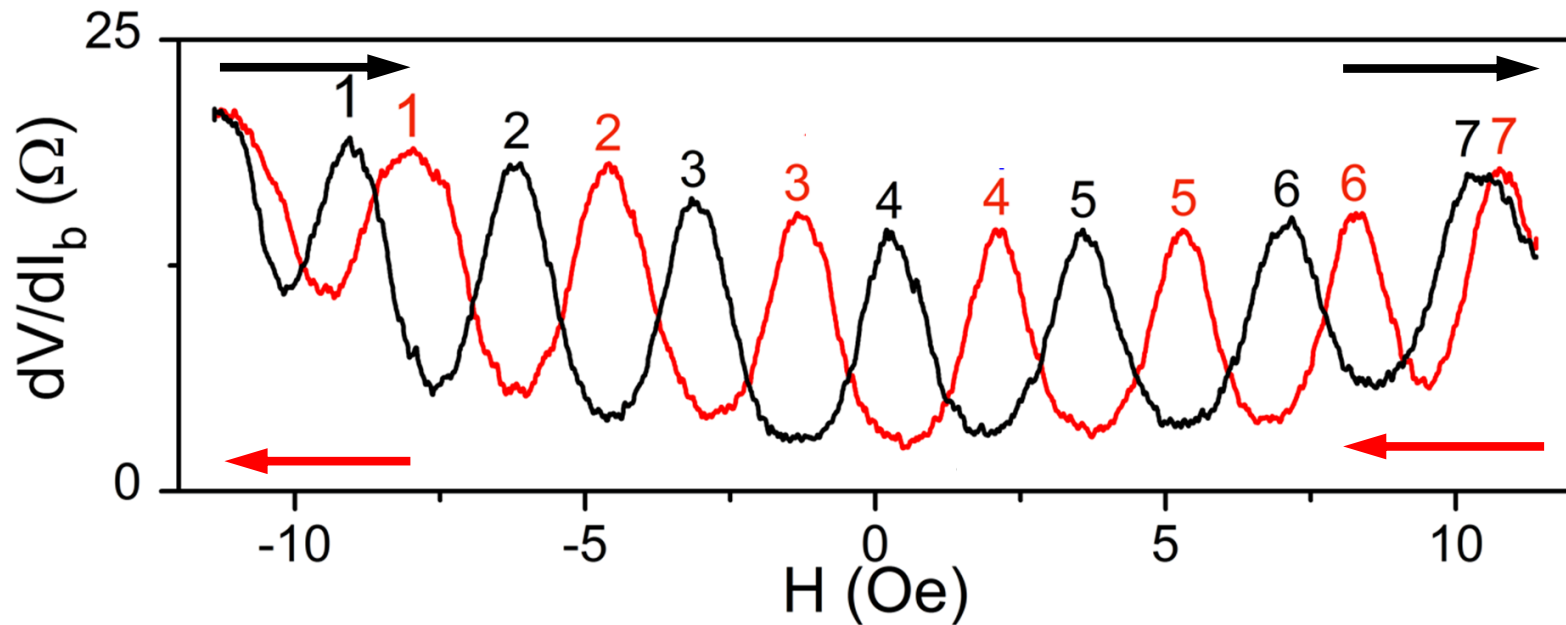




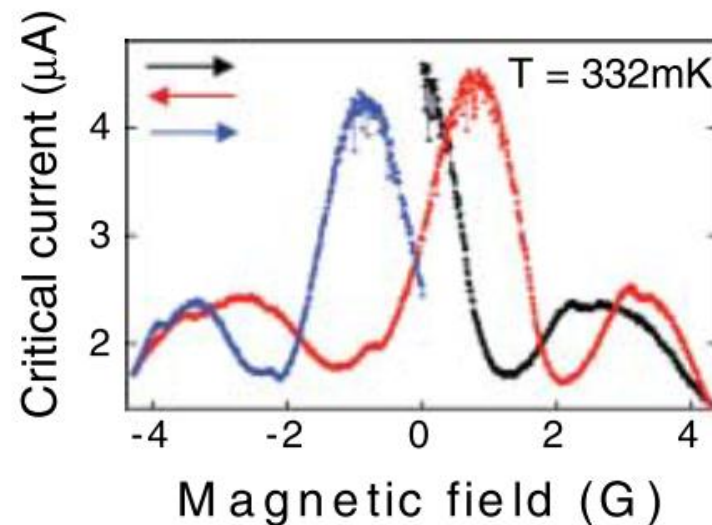
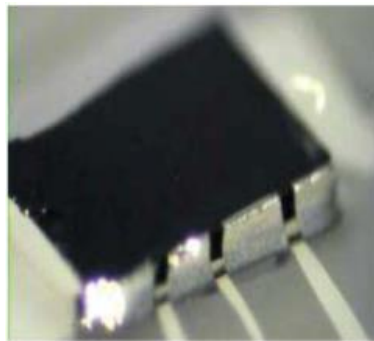
# Anomalous “advanced” hysteresis



# Anomalous “advanced” hysteresis

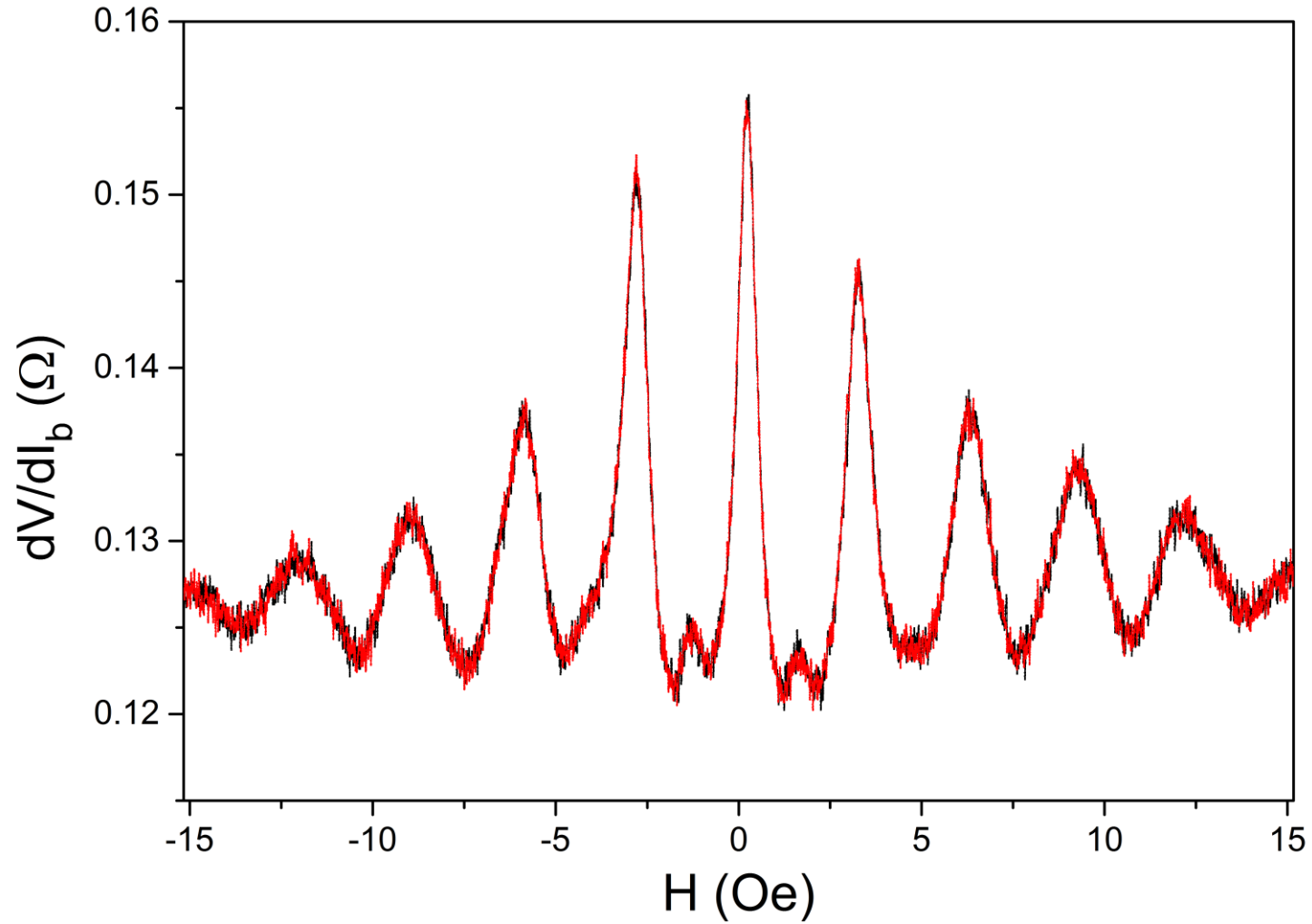


$\text{Sr}_2\text{RuO}_4$  - Pb  
Josephson Junction  
van Harlingen group  
Science 2006

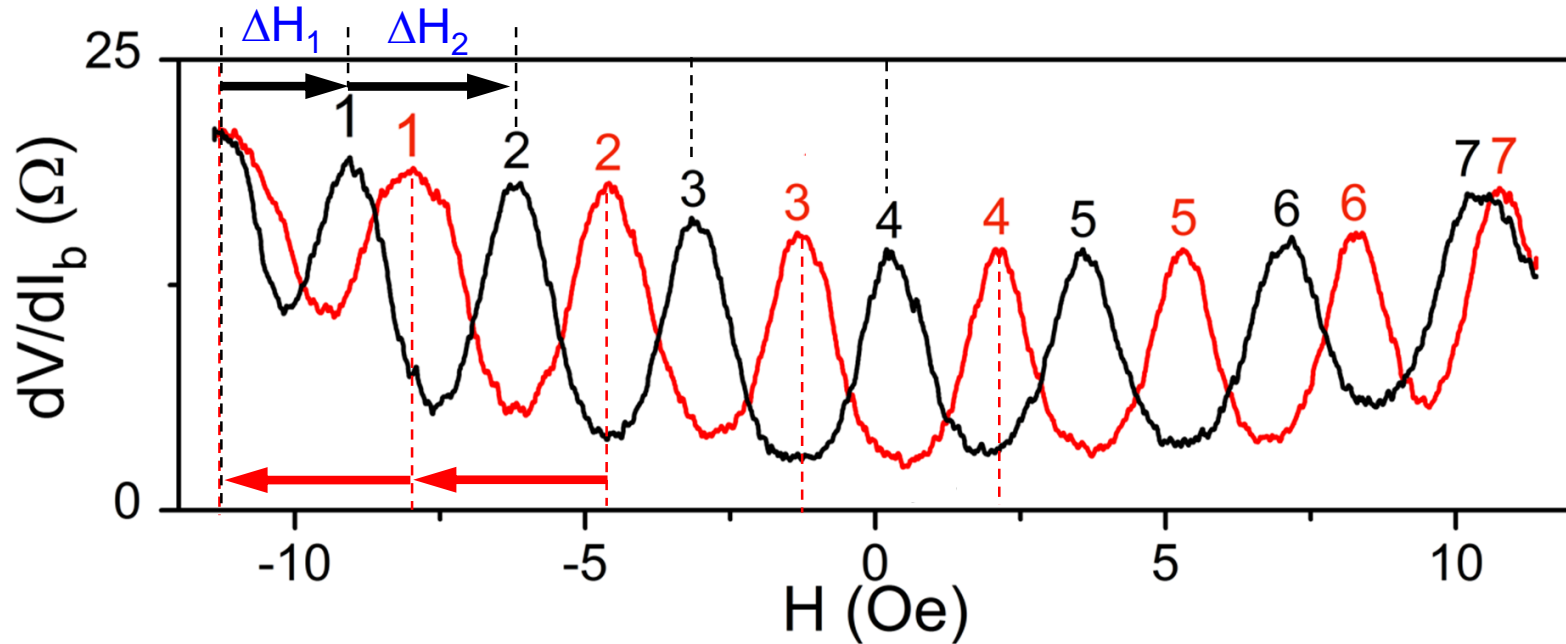


# Control Experiment

Pb-Au-Pb SQUID



# Compressed periods due to anomalous phase shift



$$I_c \propto \cos\left[2\pi \frac{(H - H_0) A_{\text{loop}}}{\phi_0} + \delta\right]$$

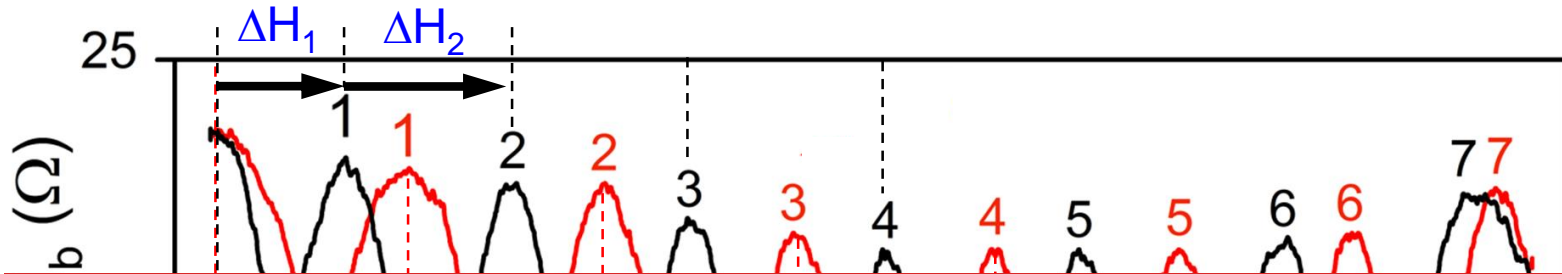
Accumulated  
anomalous  
phase shift

Compressed  
oscillation  
period

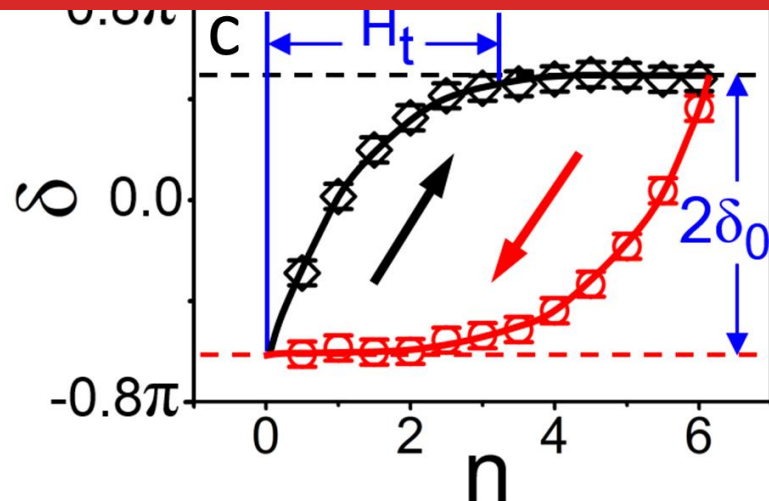
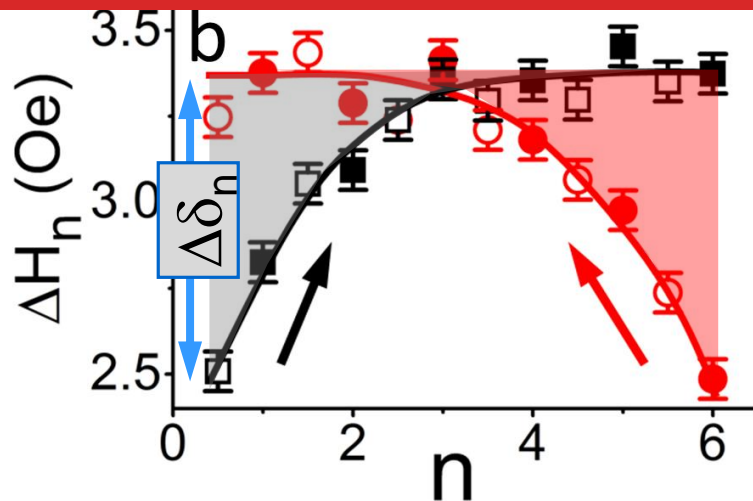
$$2\pi \frac{\Delta H_n A_{\text{loop}}}{\phi_0} + \Delta\delta_n = 2\pi$$

Anomalous  
phase shift  
in each period

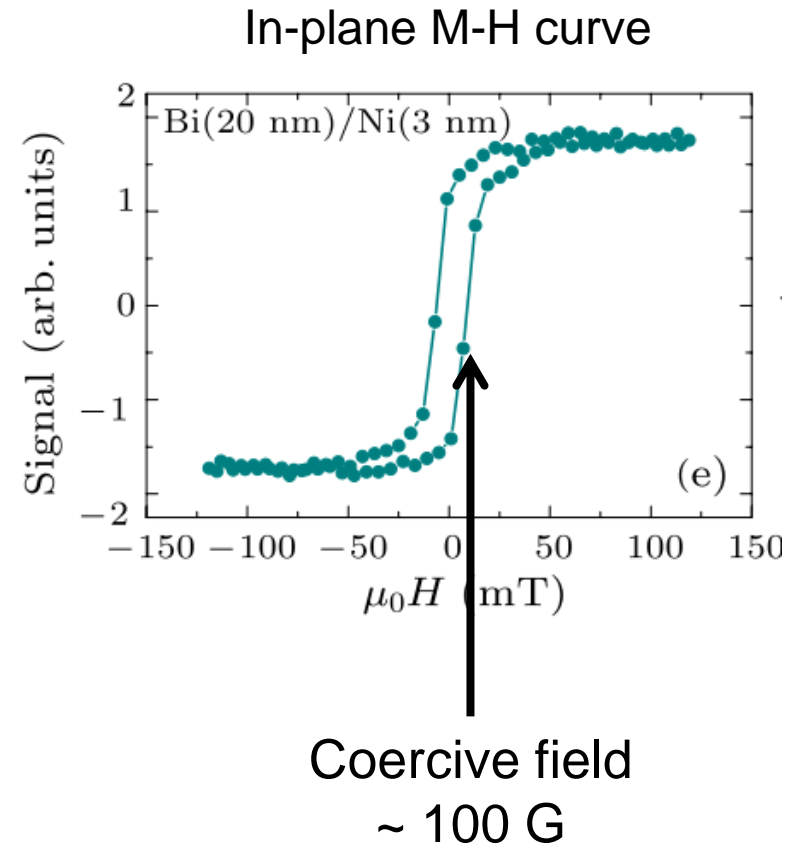
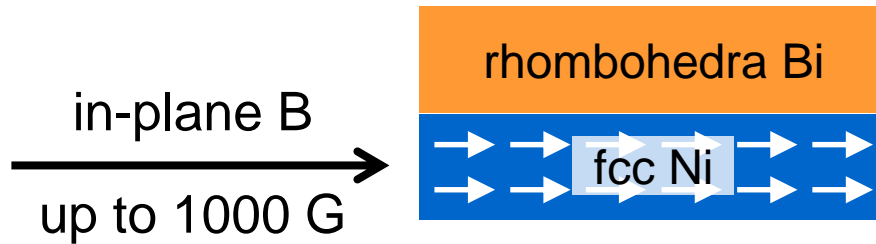
# Compressed periods due to anomalous phase shift



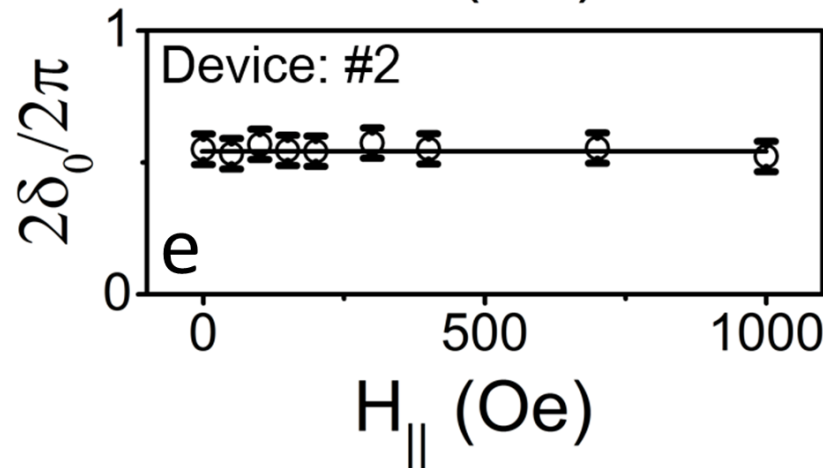
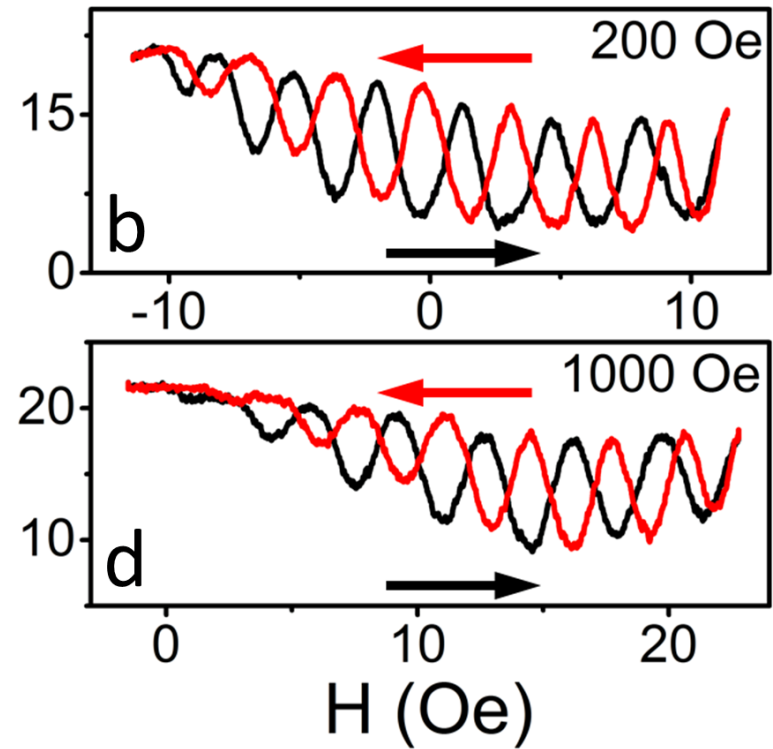
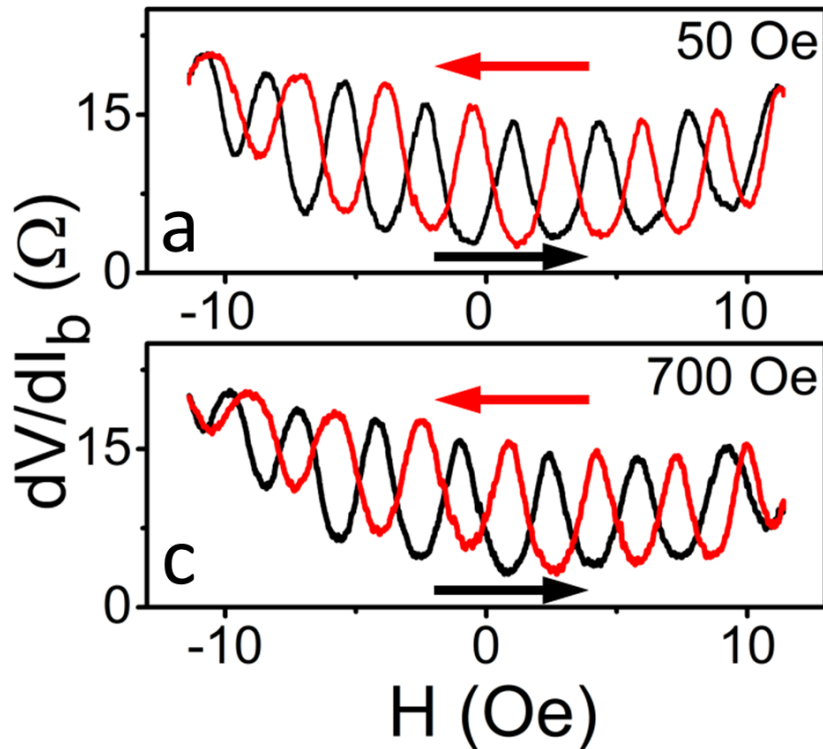
The hysteresis loop is clockwise, which is “anomalous”, being qualitatively different from the *ccw* ones for FM and flux pinning.



# Is the anomalous hysteresis related to or influenced by the ferromagnetic moments of itinerant electrons?



# In-plane field dependence of hysteresis



The Anomalous hysteresis is NOT related to the itinerant ferromagnetism.

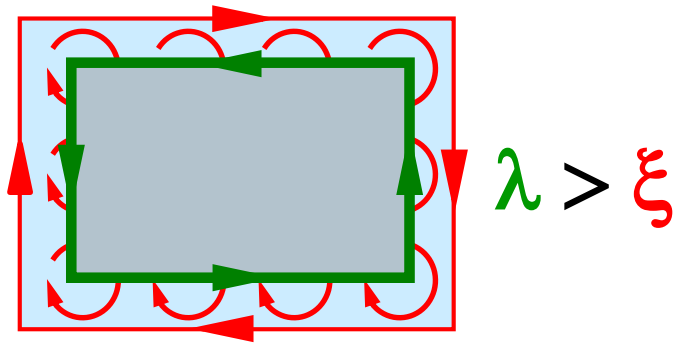
# The Picture

- Anomalous phase shift as reflected in interference  
→ anomalous flux/moments
- The anomalous moments arise from the orbital moments of the Cooper pairs.
- While the orbital moments in the bulk of SC are screened by the Meissner screening current, the moments at the edge are not.



# The Picture

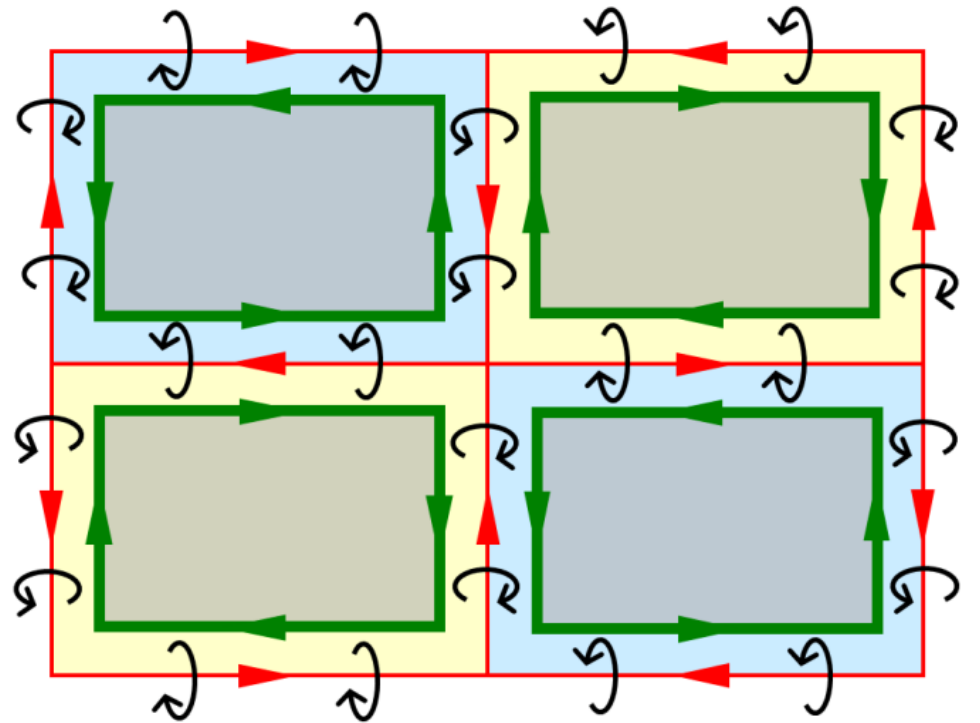
- Edge currents & Edge magnetization



M. Sigrist, T. M. Rice, K. Ueda,  
PRL 63, 1727 (1989)

high angular  
momentum pairing

- Superconducting domains

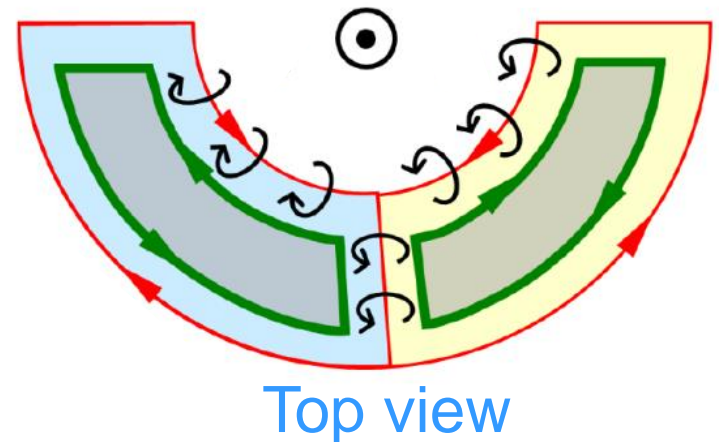
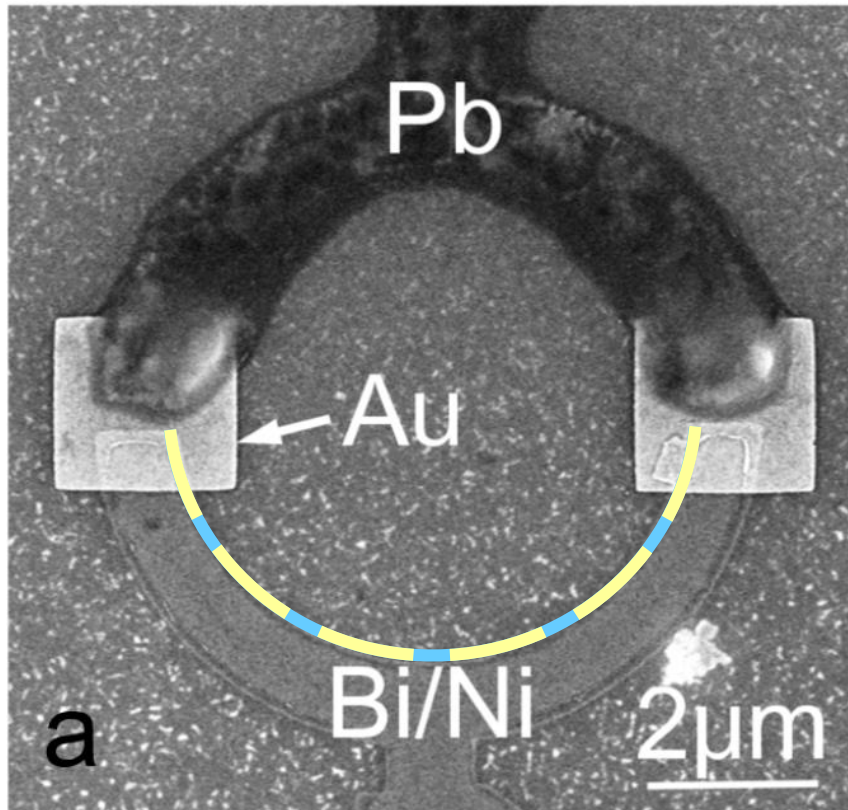


→ Domain edge current  
→ Meissner screening supercurrent  
↻ Flux lines of orbital magnetic moments

# Design of the experiment

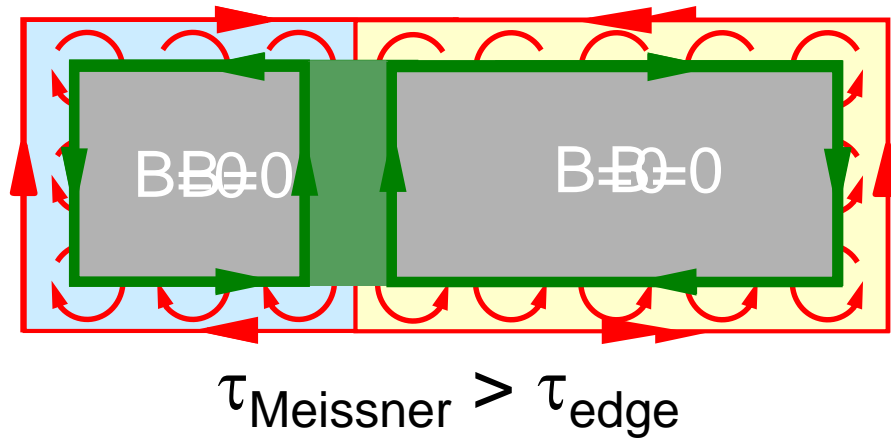
Using Bi/Ni bilayer itself to form SQUIDs, to search for out-of-plane magnetic moments at the edges

dc SQUID

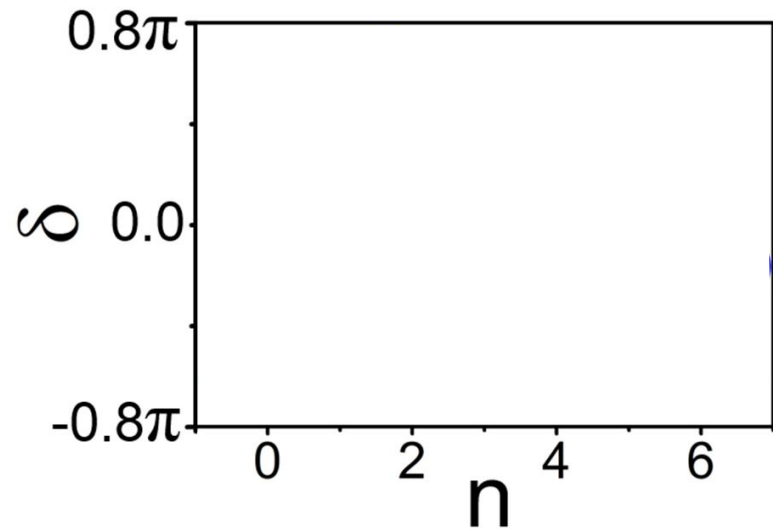
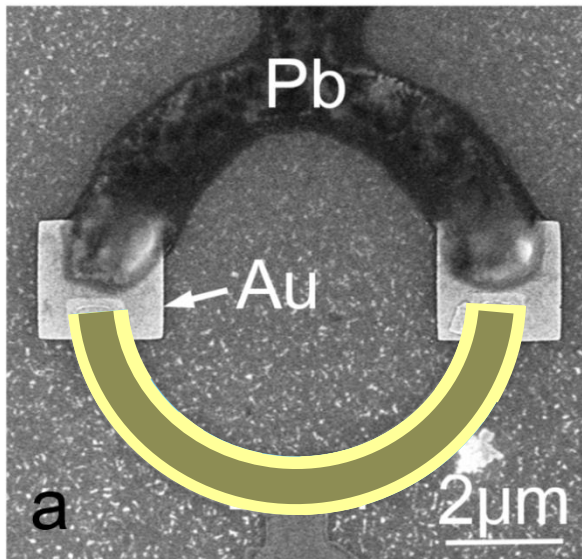
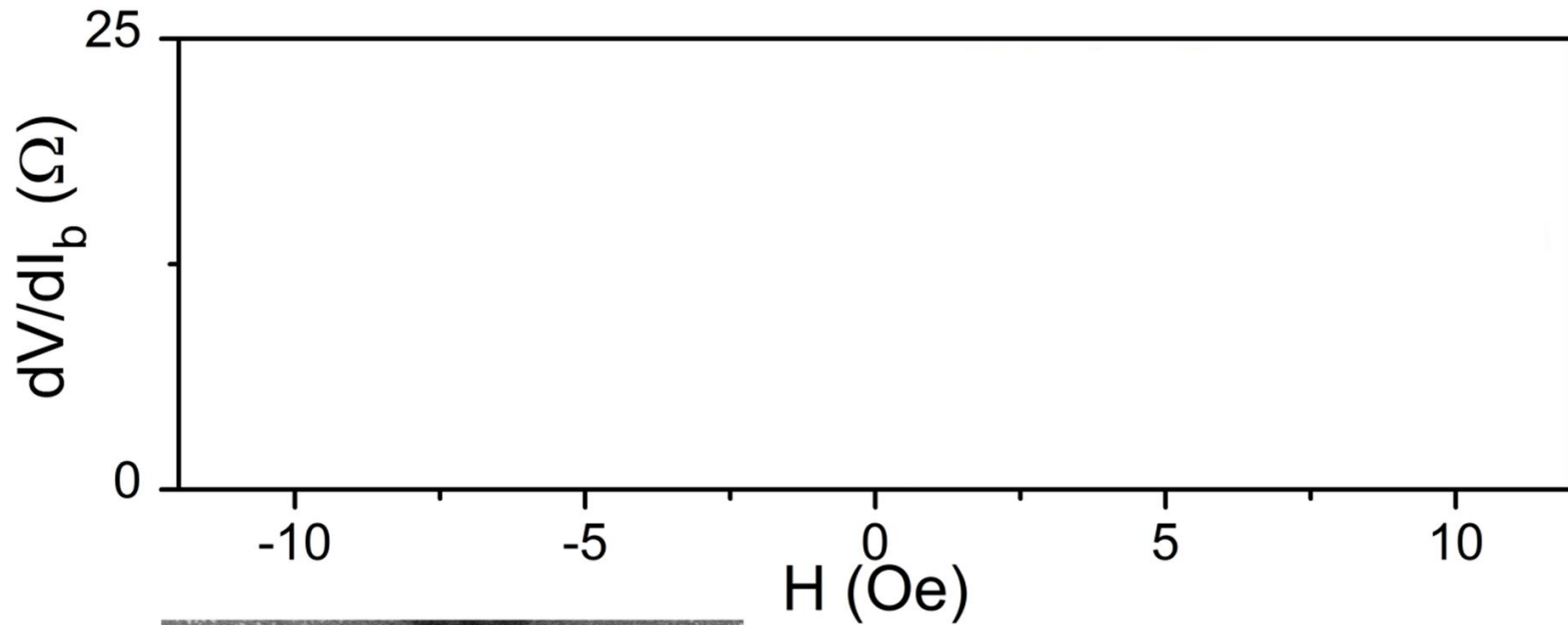


# The Picture

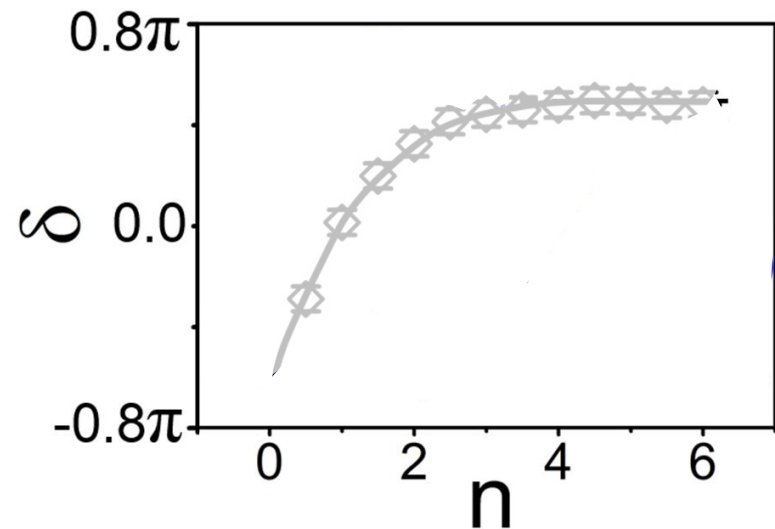
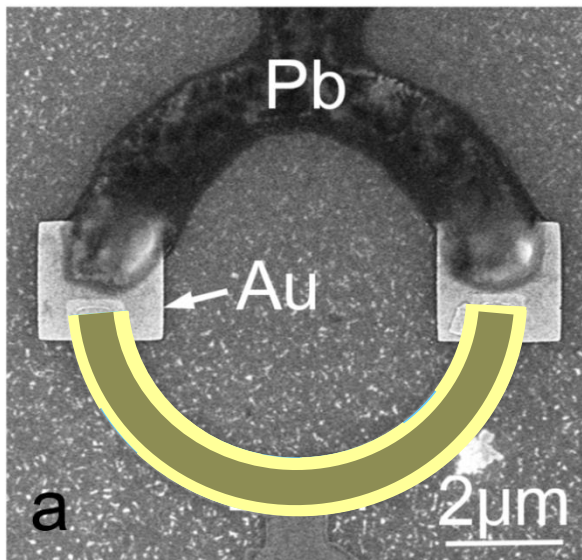
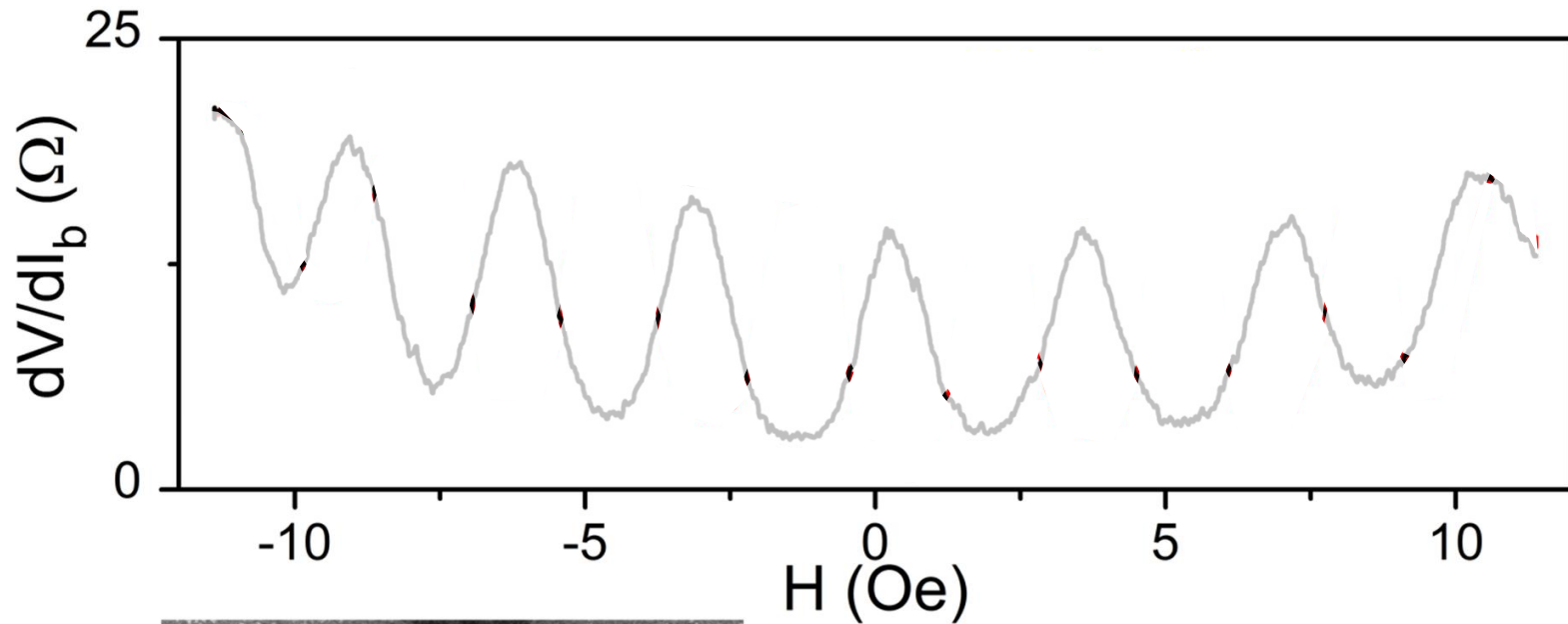
- The “advanced” hysteresis is related to the SC domain wall motion, triggered by  $\Delta B$  instead of by  $B$ .



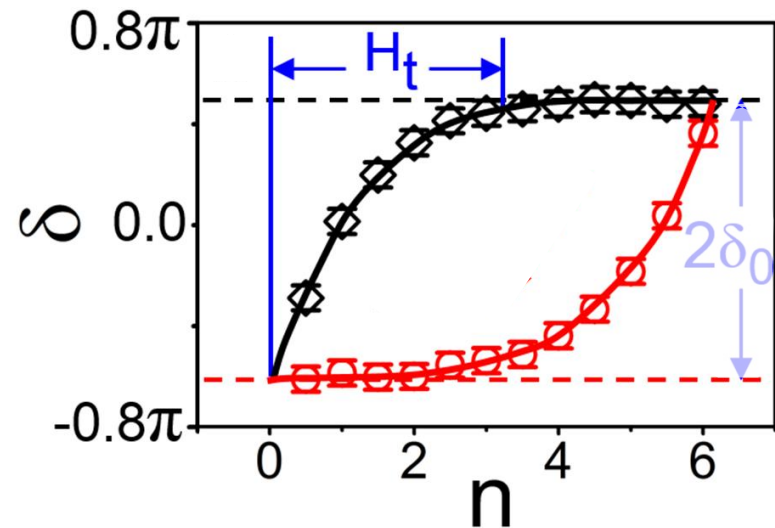
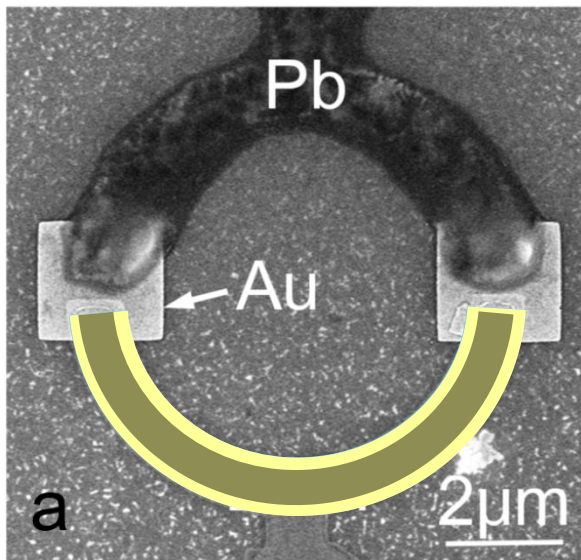
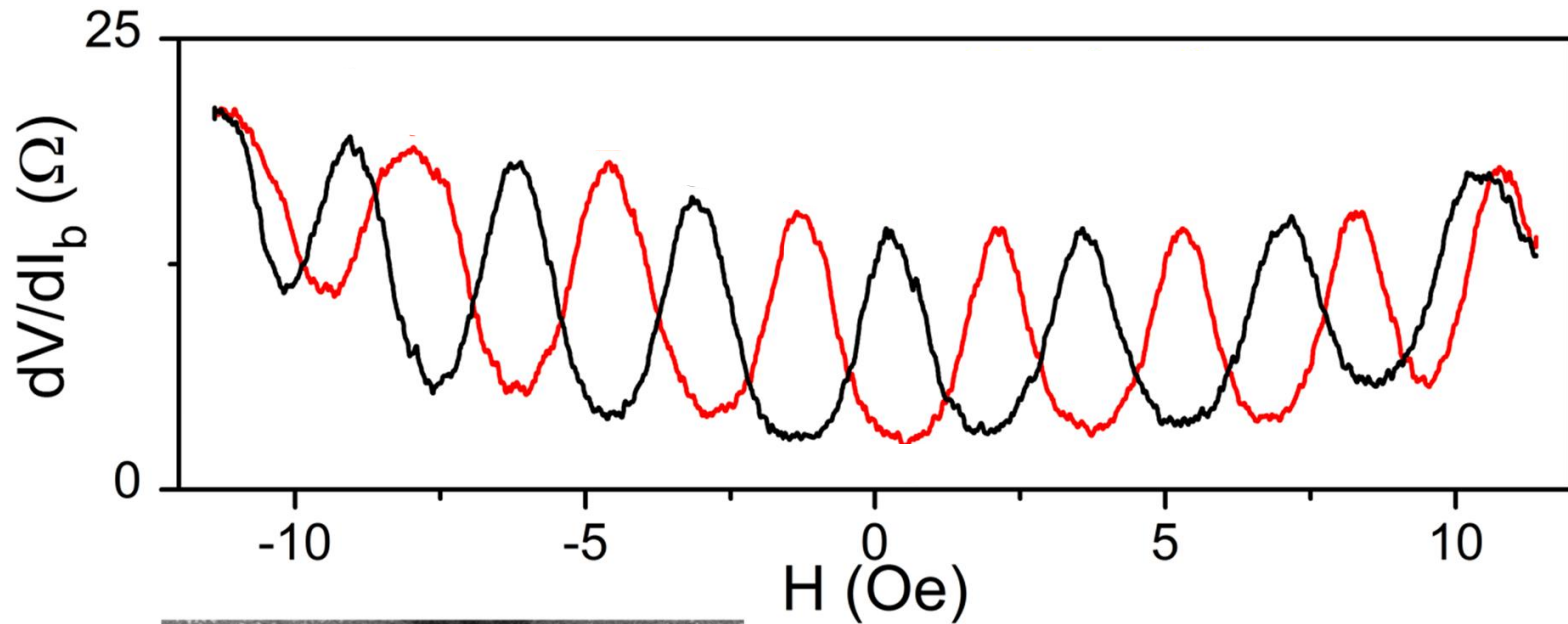
# The Picture



# The Picture for “Advanced” Hysteresis



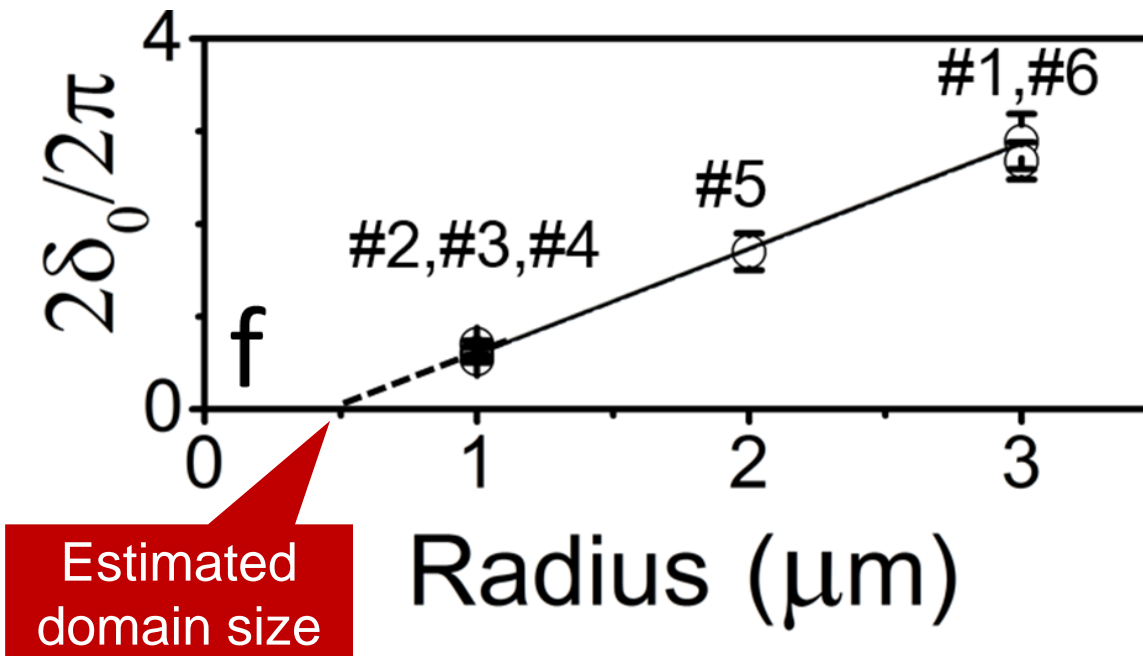
# The Picture for “Advanced” Hysteresis



# The anomalous phase shift is proportional to the perimeter of the Bi/Ni ring

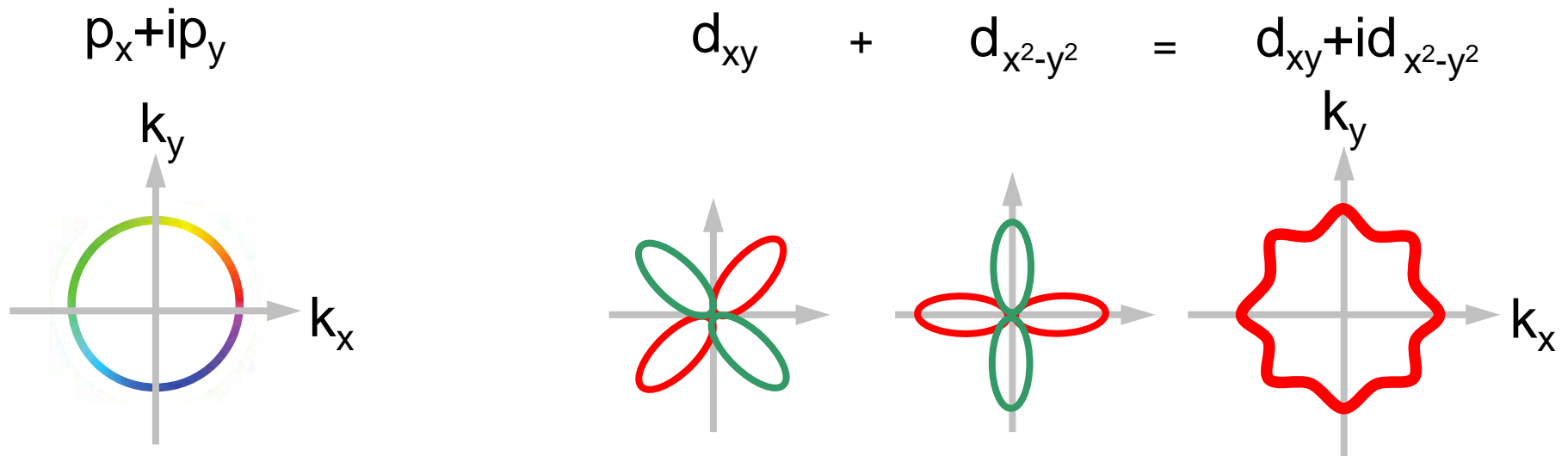
TABLE I: A list of the parameters of six devices investigated.

Device	Distance* ( $\mu\text{m}$ )	Inner Radius ( $\mu\text{m}$ )	Loop Area ( $\mu\text{m}^2$ )	Calculated Period (Oe)	Measured Period (Oe)	$2\delta_0/2\pi$
#1	0.4	3.0	39.3	0.53	$0.55\pm 0.03$	$2.89\pm 0.01$
#2	0.5	1.0	6.2	3.34	$3.37\pm 0.06$	$0.54\pm 0.04$
#3	0.2	1.0	6.1	3.39	$3.13\pm 0.08$	$0.70\pm 0.04$
#4	-0.4	1.0	5.6	3.69	$3.5\pm 0.2$	$0.60\pm 0.07$
#5	-0.4	2.0	17.6	1.18	$1.12\pm 0.09$	$1.7\pm 0.2$
#6	-0.4	3.0	35.9	0.59	$0.58\pm 0.03$	$2.7\pm 0.2$



# Chiral-p or Chiral-d ?

SC domains, edge currents/magnetization  $\rightarrow$  Chiral superconductivity



Chauhan et al., PRL 122, 017002 (2019)  
(Armitage group, Johns Hopkins U)

Gong et al., Sci. Adv. 2017;3: e1602579  
(Yakovenko group, U. Maryland)



# Conclusion

- We have observed anomalous moments on Bi/Ni bilayer, showing “advanced” hysteresis.
- We attribute the moments to the orbital moments of Cooper pairs in chiral superconducting Bi/Ni, and attribute the hysteretic behavior to the motion of chiral superconducting domains.
- Further study is needed to identify whether the pairing symmetry is  $p_x+ip_y$  or  $d_{xy}+id_{x^2-y^2}$

Thank You